

Influence of lateral heterogeneities on strong motion shear strains: simulations in the historical center of Rome (Italy)

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Abstract

The influence of lateral heterogeneities in alluvial deposits represents a topic of particular interest in the field of urban planning and engineering design of structure and infrastructures. This work is focused on the effects of such heterogeneities on the shear strains produced within the recent alluvial deposits of the Tiber River in Rome historical center in case of the worst expected earthquake scenario. At this aim, a 3D engineering-geology model of the subsoil is used to derive 4 geological sections across the Tiber River valley as well as 48 soil columns in order to perform numerical simulations. Various models are considered: a viscoelastic equivalent linear rheology in a 1D finite difference model for one motion component (EERA code), a nonlinear elasto-plastic model in a 1D finite element scheme for three motion components and a nonlinear visco-elasto-

25 plastic rheology in a 2D finite difference model under one-component horizontal input. As it results
26 from comparing these different simulations, the lateral heterogeneities play a key role with respect
27 to the expected shear strains within multilayered soils. At this aim some specific indexes are
28 introduced to estimate the maximum shear strain concentration index within the soil layers as well
29 as to highlight their effect due to the stratigraphic position of the layers, within the soil column,
30 independently from its depth. A final differential index leads to the evaluation of the lateral
31 heterogeneity effect on the estimated maximum shear strain, demonstrating their prevalent role with
32 respect to the bedrock shape (i.e. the angle of inclination of the buried valley slopes). From these
33 results, a maximum shear strain zoning map is obtained for the historical center of Rome, showing
34 that the local seismic response should be modeled by assuming 1D or 2D conditions depending on
35 the location considered.

36 **Keywords**

37 Lateral heterogeneities, strong motion, site effects, earthquake-induced strains, numerical modeling,
38 Rome

39

40 **Introduction**

41 Local seismic response in large urban areas is often estimated through one-dimensional (1D) and
42 two-dimensional (2D) numerical simulations (Rovelli et al., 1994, 1995; Panza et al., 2004;
43 Bozzano et al., 2008; Bonilla et al., 2010; Bonilla et al., 2006; Bouden-Romdhane et al., 2003;
44 Semblat and Pecker, 2009). During the last decades multi-dimensional seismic wave amplification
45 have been pointed out in different basins from noise and weak-motion records. This topic is
46 particularly important in urban areas where the original morphology of the natural valley can be
47 hidden also by the presence of human structures and infrastructures (Rassem et al., 1997; Semblat et
48 al., 2000, 2002; Bouden–Romdhane et al., 2003; Kham et al., 2006; Sørensen et al., 2006; Semblat

et al., 2008). 2D amplification effects can be detected by seismometric measurements but a significant effort needs to be done to relate them to geological constraints (Di Giulio et al., 2008; Lenti et al., 2009), especially in the case of heterogeneous valley fills or of irregular bedrock geometries. In this regard, previous studies were mostly focused on the effects related to the impedance contrast among horizontal layers, i.e. few researches were devoted so far on the contrasts due to the existence of lateral contacts among different lithologies (Semblat et al., 2005; Peyrusse et al., 2014). In cases where superficial seismic measurements are not suitable since they are not representative for free-field condition as a consequence of site-city interaction effects (Kham et al., 2006; Semblat et al., 2008) and records from vertical seismic arrays are not available, an important role can be played by numerical models able to account for basin effects, i.e. multi-dimensional geometries and lateral soil heterogeneities.

The use of numerical methods is widespread; some experiments have demonstrated the reliability of these numerical approaches in reproducing observed local seismic effects also for irregular geometries of the fill deposits and the bedrock (Semblat et al., 2002a,b). Moreover, numerical modeling makes it possible to obtain transfer functions resulting from bedrock/outcrop ratios in both linear and nonlinear conditions (Lanzo and Silvestri, 1999) or amplification functions resulting from outcropping-fill/outcropping-bedrock ratios (Borcherdt, 1994). More recently, the percentage of non-linearity (PNL) and the associated shift frequency (f_{sh}) parameters were introduced by Regnier et al. (2013) to describe and estimate the effects of soil nonlinear behaviour on site response.

The numerical methods were mainly devoted to analyse possible local effects due to the modification of the input seismic wavefield in the superficial layers, both in linear and non-linear conditions. The numerical models (Bard, 1983; Bard and Bouchon, 1980a, b, 1985; Mozco and Bard, 1993; Pergalani et al., 1999; Makra et al., 2005; Semblat et al., 2005; Pergalani et al., 2008; Lenti et al., 2009; Gélis and Bonilla, 2012; 2014) demonstrate that in case of basins-like systems filled by homogeneous and heterogeneous deposits, local seismic response depends on many

75 features such as soil geometry, impedance contrast, dynamic properties, as well as on the stress field
76 variations induced by the seismic motion that may lead to relevant nonlinear effects.

77 Among the effects related to the local seismic response, the study presented herein focuses on the
78 analysis of earthquake-induced strains, within soil deposits that fill a basin-like system, by taking
79 into account the heterogeneities due to both lateral and vertical contacts. In this regard, a nonlinear
80 soil behaviour should be considered where the most severe expected earthquake scenario. At this
81 aim, we propose an approach based on the comparison among different numerical modeling
82 solutions to elicit the contributions due to 1D vs. 2D effects, linear vs. nonlinear soil behaviour. The
83 effects of a multiaxial stress state in the soil, modeled by a 3D-rheology, are also investigated since
84 they can play a significant role on the resulting nonlinear strains (Santisi d'Avila et al., 2012, 2013).
85 Moreover, this study is particularly focused on the maximum shear strain distribution in the Rome
86 historical centre, to get an insight for possible interaction with structure (i.e. foundations or
87 infrastructures) by mapping where 1D approximation is sufficient to assess maximum shear strain
88 and where prevalent 2D effects control.

89 The recent alluvial plain of the Tiber River in the historical center of Rome (Italy) was selected as
90 study area (Fig.1) for this research because of the relevance of the historical heritage, the
91 documented historical damages on both monuments and buildings related to the historical strong
92 earthquakes (Ambrosini et al., 1986; Molin and Guidonboni, 1989; Donati et al., 1999; Donati et
93 al., 2008; Bozzano et al., 2011) as well as for the geological and geotechnical data availability from
94 previous studies (Bozzano et al., 2000; Bozzano et al., 2008; Raspa et al., 2008) (Fig. 1).

95 Rome is located at a distance of some tens of kilometers from the central Apennines seismogenic
96 zone, where earthquakes of tectonic origin and of a magnitude up to 7.0 can be expected (Fig.1).
97 The most recent major earthquake occurred on April 6th, 2009 (Mw 6.3) close to L'Aquila city,
98 about 100 km northeast (NE) from Rome (Blumetti et al., 2009) and was felt in Rome up to V MCS
99 intensity. Smaller earthquakes, with a focal depth less than 6 km and maximum magnitude of 5,

originate at the Colli Albani hills volcanic source (Amato et al., 1994). Moreover, a local seismicity in the urban area can produce earthquakes with a magnitude below 4 (Tertulliani et al., 1996); these smaller events are expected to produce a maximum intensity of VI to VII in Rome.

Several studies on the local seismic response in Rome are already available in the literature. Rovelli et al. (1994; 1995) performed 2D finite difference simulations and a hybrid technique based on summation and finite differences was proposed by Fäh et al. (1993). This model was designed assuming a homogeneous fill of the Tiber River valley, except for a basal layer of gravels on the local seismic bedrock, and a viscoelastic rheology attributed to the alluvial soils. Olsen et al. (2006) generated a 3D velocity model for Rome embedded in a 1D regional model, considering a homogeneous fill of the Tiber River valley, and estimated long-period (>1 s) ground motions for such scenarios from finite difference simulations of viscoelastic wave propagation. This model confirmed a 1Hz resonance frequency for the alluvial deposits while pointed out durations much longer than those from previous studies that omitted important wave-guide effects between the source and the city. Bozzano et al. (2000; 2008) analyzed static and dynamic geomechanical properties of the Holocene alluvial fill within the Tiber River valley and demonstrated that the silty-clay deposits, representing the most part of the Tiber alluvial body, play a key role in assessing the soil column deformation profile since it can be affected by nonlinear effects induced by the maximum expected earthquake. The first seismic ground-motion recorded in the urban area of Rome (at the Vasca Navale array) corresponds to the April 2009 L'Aquila seismic sequence (Caserta et al., 2013); the empirical soil transfer function shows a significant amplification at almost 1Hz according to the 1D simulations already obtained for the same site (Bozzano et al., 2008).

Rome historical centre is a good case study to assess the role of 1D vs 2D effects as it regards the shape ratio of the bedrock in the Tiber River valley. According to Bard and Bouchon (1985), the computed values are always lower than 0.3 and therefore suitable for a 1D resonance combined to lateral wave effect. Moreover, according to Semblat et al. (2010) amplification lower than 20

125 should be expected in the Tiber river valley at the fundamental frequency of about 1Hz under
126 perfectly elastic conditions. This results by considering a κ_h ratio ($=L/H$ where L = half length of the
127 valley and H is the maximum depth) much more higher than 6 and impedance ratio χ parameter
128 ($=V_{s_bedrock}/V_{s_soft\ soil}$) ranging from 1 to 2.

129 **The Rome historical center case study**

130 Rome is one of the main historical cities of Italy and its political center. The millenary history of the
131 city, its extraordinary historical heritage and the actual population of about 4 millions inhabitants
132 entails a high vulnerability and exposure to natural risks. The actual geological setting of Rome
133 urban area results from a recent evolution of the Tiber River alluvial valley connected to the
134 adjacent coastal plain. Nonetheless, this evolution represents the final stage of the geodynamic
135 processes responsible for the genesis of the Central Apennines chain (Fig. 1). Several studies
136 contributed so far to the reconstruction of the geological setting of Rome subsoil (Corazza et al.,
137 1999; Bozzano et al., 2000; Campolunghi et al., 2007; Bozzano et al., 2008; Raspa et al., 2008;
138 Milli et al., 2013, Mancini et al., 2013).

139 The area of Rome historical center is characterised by marine sedimentary conditions from Pliocene
140 through early Pleistocene times (4.5-1.0 myr). This Plio-Pleistocene succession consists of
141 alternating, decimetre-thick layers of clay and sand, with an overconsolidation ratio (OCR) greater
142 than 5 and low compressibility (Bozzano et al., 1997). Given its lithological features, the Monte
143 Vaticano Unit (UMV) is considered to be the geological bedrock of the area of Rome. During
144 middle-late Pleistocene and Holocene, the sedimentary processes were confined to fluvial channels
145 and coastal plains and strongly controlled by glacio-eustatic sea-level changes (Karner and Renne,
146 1998; Karner and Marra, 1998, Marra et al., 1998). At the same time, this area also experienced
147 strong volcanic activity, which caused the emplacement of a thick pyroclastic cover that became
148 intercalated into the continental sedimentary deposits.

149 The current hydrographic network of the Tiber valley and its tributaries, were originated from the

150 Würm glacial period (18 kyr) and it results from re-incision and deepening of valleys hereditated
151 from the previous glacial-interglacial phases.

152 The sediments partially filling the Holocene valleys (Bozzano et al., 2000) are generally
153 characterised by a fining-upward succession, with a few meters thick basal layer of gravels grading
154 into a thick pack of sands and clays (Fig. 2). This fine-grained portion of the deposit is represented
155 by normally to weakly overconsolidated clayey and sandy silts, saturated in water, with low
156 stiffness. According to Bozzano et al., (2000), the alluvial deposits were distinguished in 7
157 lithotechnical units, in the following named “layers” for simplicity. Figure 2 shows a basal G layer
158 is constituted of coarse grained deposits, up to 10 m thick, covering the UMV and composed of
159 limestone gravel in a grey sandy-silty matrix. The D layer is composed by grey coloured silty-sands
160 passing to clayey-silts. These layers were recently distinguished in two sub-layers (Bozzano et al.,
161 2012): the D1 sub-layer characterised by a prevalent sandy grain size; the D2 sub-layer
162 characterized by a prevalent silty-clay grain size. The C layer is composed by grey clays passing to
163 silty-clays with a variable organic content which is responsible for local dark colour; this layer is
164 mainly located close to the boundary of the valley and, in particular, on its right side, where it
165 reaches a maximum thickness of about 50 m.

166 The clayey C layer is locally carved by some furrows filled by the B layer, which is generally
167 composed by brown to yellow coloured sands (B1) and locally passes to silty-sands and clays (B2).
168 The recent alluvia of the Tiber (A level) complete the sedimentary succession; these alluvia are
169 mainly composed of silty-sands locally passing to clayey-silts, up to 15 m thick, in correspondence
170 to the left side of the valley.

171 Finally, the R layer, up to 8 m thick, represents man-made fills, i.e. the most recent deposits which
172 overly the Tiber alluvia and they are characterised by abundant, variously sized brick fragments and
173 blocks of tuff embedded in a brown-green silty-sandy matrix, also including ceramic and mortar
174 fragments.

175

176 Based on the geomechanical characterisation by Bozzano et al. (2000; 2008), the C layer is
177 classified as inorganic silty-clay of average-high compressibility with a very low OCR of about 1.2,
178 whereas the UMV are defined as stiff silty-clays ($OCR \cong 6$). Lithotypes A and D2 are defined as
179 silty-clays with middle-low compressibility. Based on oedometer tests, the A layer clayey silts are
180 highly overconsolidated ($OCR \approx 10$), probably due to changes in the water table position.

181 The B1 layers is characterised by sand, sandy loam and sandy-clayey loam while the B2 layer is
182 predominantly characterised by sandy loam, sandy-clayey loam with subordinate silty clay and clay
183 of low to medium plasticity. The D1 sub-layer includes deposits with a sandy-silty grain size which
184 were differentiated with respect to the silty-clayey D2 sub-layer on the basis of borehole log-
185 stratigraphies as well as of available grain size distributions (Bozzano et al., 2012).

186 Site and laboratory testing of the Tiber alluvial deposits (Bozzano et al., 2008), demonstrated that a
187 significant difference exists between sandy or silty-clayey deposits (A, B, C, D layers) and the
188 basal sandy gravels (G layer). In terms of shear wave (S-wave) velocity (V_s) the above mentioned
189 difference corresponds to a ΔV_s of about 300 m/s (Fig.3a). In this regard, the G layer can be
190 considered as the local seismic bedrock, since it has a $V_s > 700$ m/s (Bozzano et al., 2008).

191 Relatively low V_s values (< 600 m/s) were measured within the first 10 m of UMV; this finding is
192 consistent with a softening effect related to the stress release caused by the late Pleistocene fluvial
193 erosion (Bozzano et al., 2006). As a consequence, linearly increasing V_s values (e.g., from 540 up
194 to 1000 m/s) have been assumed in the numerical models in the first 20 meters within the UMV.

195 The dynamic properties of the Tiber alluvial deposits were derived by resonant column and cyclic
196 torsional shear tests assuming confining pressure in the range 200-300kPa (Bozzano et al., 2008).

197 At low strain levels (i.e., for strain levels where no significant reduction of shear moduli are
198 observed, strain level $< 10^{-6}$) these tests lead to a difference between the stiffness related to the
199 Tiber alluvia and the high consistency UMV clays of the bedrock equal to about 100 MPa.

200 Conversely, the differences measured inside the alluvia (i.e. between C and A layers) are less
201 significant and anyway in the 50–100 MPa range. The decay curves deduced from the same tests

(Fig.3b) put in evidence that the linearity threshold (γ_l) for the shear strains is of about 0.005% for the UMV and in the range 0.01% - 0.02% for the A and C layers of the alluvial deposits, while the volume shear deformation threshold (γ_v) for the A and C layers ranges from 0.02% to 0.05%. The D1 layer was characterised by resonant column tests on reconstituted samples (Bozzano et al., 2012). At this aim, the Proctor optimum of the granular mix was reached at a saturation of 90%, with a water content (w) of 17.6%, corresponding to a density (γ_d) of 16.70 kN/m³. Resonant-column tests yielded a γ_l of 0.005% and a γ_v of 0.03%. As it resulted from the laboratory tests, seven G/G₀ and D vs. shear strain curves were associated to the lithotechnical units as reported in Fig.3b.

According to the resonant column tests, a hysteretic constitutive law was attributed to layers with $V_s < 800$ m/s; whereas a viscoelastic constitutive law was attributed to the other UMV layers (Fig.3).

214

215 Numerical models

216 *3D engineering-geology model of the subsoil*

A 3D engineering-geological model of the alluvial fill in Rome historical center was reconstructed based on log-stratigraphies from 78 boreholes collected so far from literature studies and technical reports (Fig.4). The depths reached by these boreholes range from 30 up to 67 m b.g.l. and 28 reach the high-consistency clays of the UMV geological substratum. The 3D model reconstruction was performed by co-relating and interpolating the borehole stratigraphies on different planes with a depth interval of 5 m and by obtaining a vertical correlation among them (Fig.4a). The engineering-geology model was obtained by differentiating the lithotechnical units (cfr. § 2.2) and by deriving their geometries within the alluvial fill, i.e. by describing the vertical and horizontal contacts existing among them. Based on the 3D geological model, 12 cross sections were derived all along the Tiber River valley (displayed in Fig.1) and 48 soil

columns were extracted along these sections. To identify the 48 columns selected along the sections a binomial label was attributed that reports the Arabic number of the section and a capital letter indicating the position of the column along the section as reported in Fig.1 (for example the 1A soil column is located along section 1 at position A). As displayed in Figs.4b and 4c, the 12 sections extracted from the 3D engineering-geological model were smoothed in order to be used for the related numerical models.

Both geological cross sections and soil columns show the high heterogeneity of alluvial deposits that fill the Tiber River valley in Rome historical center. In particular, the 3D engineering-geological model points out that (Figure 4): the G layer is always present at the basis of the deposits, the D1 layer is generally centered with respect to the valley; the C layer fills the most part of the valley and it is inter-layered with D2 layer; the B1, B2 and A layers are distributed within the first 25 m b.g.l.. From the considered soil columns it is obvious that the most part of the fill is constituted by the inorganic clays ascribable to the C layer (i.e. almost 33% of the cumulative thickness of the alluvial deposits along the considered columns that is of about 3km as shown in Fig.5a) whose thickness varies up to 50 m (see thickness distribution in Fig. 5b).

Reference input motion

For this study a unique three component time history representative for the maximum ground motion expected in the historical center of Rome at 475 years was considered. The reason of such a choice is that a deterministic approach for the earthquake-induced strain effects was adopted following previous studies on the seismic response in the Rome historical center (Rovelli et al., 1994; 1995; Olsen et al., 2006). In addition, a previous study by Bozzano et al. (2008) shows that inputs representative for other seismogenetic sources (such as the Colli Albani one) are not suitable for producing non linear effects within the alluvial soils of the Tiber river in the Rome urban area. No synthetic inputs were used, in agreement with the present Italian technical rule for geotechnical constructions, but time history selected among several

natural accelerometric records collected in the European Strong-motion Database (ESD). Moreover, to avoid that specific features of the seismic input could influence the modelled seismic response, the spectral content of the selected time history was checked to have a regular distribution in a wide frequency range (0.1-10Hz).

It was not possible to consider the acceleration time history of the 2009 L'Aquila mainshock recorded by the vertical array of Valco S. Paolo station in Rome (Caserta et al., 2013) since the measured peak of ground acceleration (PGA) was around $10^{-3}g$ that is two orders of magnitude lower than the current study. As a consequence, a three-component time history has been produced (Bozzano et al., 2012), taking into account the maximum PGA expected in the historical center of Rome (i.e. 0.1258g at 475 years according to the project INGV-DPC 2004-2006). As a first step, a historical analysis of the felt seismicity was performed by considering the last 2000 years, obtaining a couple of (magnitude-distance) values representative for the maximum seismic scenario expected in Rome. These parameters allowed to select from the European Strong-motion Database (ESD) a first set of three-component time histories, representative of the maximum expected ground motion. As a second step, the response spectra (5% inelastic damping) related to these time histories were calculated and compared to the reference response spectrum expected for Rome. The latter is already available and defined in the framework of the national project UHS INGV, Cluster 6, Central Italy. The best fit allowed selecting only one three-components time history among the whole set of data selected starting from the ESD. The horizontal component with the maximum ground acceleration value was scaled to the characteristic PGA value for the historical center of Rome. The other components were then scaled taking into account the ratios between the PGA of the three original time histories. This procedure allowed obtaining three acceleration time histories representative for the maximum ground motion expected in Rome and which were used in the numerical modeling (Fig. 6).

1D numerical models

The relevance of 1D modelling consist in providing transfer functions as well as the maximum shear strain (MSS) distribution with depth that can reveal the role of the vertical heterogeneities (i.e. layering) of the subsoil also depending on the non linear effects in case of strong motion (Bonilla et al., 2011; Regnier et al., 2013) . In this study the 1D modeling was performed for the 48 selected soil columns (Table 1), using two 1D numerical wave propagation models, an equivalent linear model (EERA code by Bardet et al., 2000) and a truly nonlinear approach (SWAP_3C code by Santisi d'Avila et al., 2012), and the time histories obtained by the previous procedure. In particular, EERA allows evaluating the local seismic response of horizontally stratified soil to the one-directional wave propagation of one-component vertically incident waves, considering the equivalent linear approach in the frequency domain. Conversely, SWAP_3C can model the one-directional propagation of a three-component ground motion in a soil profile. In the SWAP_3C code, the three-dimensional nonlinear cyclic elastoplastic constitutive model, originally proposed by Iwan (Iwan, 1967; Joyner, 1975; Joyner and Chen, 1975) for dry soils, is implemented in a finite element scheme. Iwan's constitutive relationship, defined as a Masing-Prandtl-Ishlinskii-Iwan (MPII) type model by Segalman and Starr (2008), has been selected because few parameters commonly available (density and shear modulus decay curve) are necessary to characterize the soil hysteretic behaviour (Santisi d'Avila et al., 2012). The MPII model is nonlinear in loading and unloading. Shear and pressure seismic waves are simultaneously propagated along the vertical z -direction in a nonlinear soil profile, from the top of an underlying semi-infinite elastic seismic bedrock to the free surface. The stresses normal to the free surface are assumed null and an elastic boundary condition is imposed at the soil-bedrock interface (Joyner and Chen, 1975; Bardet and Tobita, 2001), in terms of stresses normal to the soil column base, allowing energy to be radiated back into the underlying medium, to take into account the finite rigidity of the bedrock. The multilayered soil

is assumed of horizontal infinite extent, with consequent no strain variation in horizontal directions x and y . At a given depth, soil is assumed to be a continuous and homogeneous medium.

This procedure can be used to evaluate the role of geotechnical and ground motion parameters affecting the soil response.

2D numerical models

2D models are relevant since they point out amplification effects due to horizontal heterogeneities (due to heteropy or unconformity of lateral geological contacts) in terms of amplification functions ($A(f)$) as well as of MSS distribution within the alluvial body. In this regard both the $A(f)$ and the MSS distribution can be influenced by the basin shape, the impedance contrast between soft soil and bedrock (Bard and Bouchon, 1985; Lenti et al., 2009; Semblat et al., 2010) and the non linearity effects in case of strong motion (Bonilla et al., 2005; Assimaki and Li, 2012; Gélis and Bonilla, 2012; 2014). In this study, the 2D numerical modeling was carried out on 4 among the 12 available cross sections realised across the Tiber River valley in Rome historical center (Fig.7). These selected cross sections (1, 6, 7 and 11) are representative of the alluvial fill deposit main features: i) a variable position of the D1 layer with respect to the middle portion of the valley, ii) a thickness of the upper alluvial deposit that includes layers R, A and B varying in the range 10 – 30 m, iii) different lateral contacts between layer D1, D2 and C; iv) the angles of the buried valley slopes measured from the ground level to the top of the gravel varying up to 30°.

Finite difference (FD) stencil proposed by Saenger et al. (2000) is considered to model the 2D propagation of P and Vertical Shear waves (P-SV). This stencil allows computing all components of the stress-strain tensor in one point of the numerical mesh, which simplifies the implementation of the computation of nonlinear soil rheologies. Consequently wave

propagation in heterogeneous linear and nonlinear media is efficiently modelled. Furthermore, the free surface is easily introduced by zeroing Lamé parameters above the free surface and surface waves can be modeled more accurately (Gélis et al., 2005) than with traditional staggered-grid methods (Virieux, 1986).

The models are 90 m deep and almost 4 km wide; nevertheless, the domain corresponding to the basin of each section profile was laterally extended in order to have a numerical reference in the model so that rock outcropping motions can be obtained. Furthermore, absorbing boundary conditions are guaranteed at the bottom and the sides of the model.

In this study, attenuation for all linear simulations was introduced by using the method proposed by Day and Bradley (2001). The minimum values of the quality factor for S-waves (Q_S) was directly derived from the V_s values if not directly inferred them from the Resonant Column laboratory tests. The values of the quality factor for pressure waves (P-waves) (Q_P) were assumed equal to $2Q_S$. The spatial and time discretizations were $dx = 0.5\text{m}$ and $dt = 5\text{e-}5\text{ s}$ which permit to have reliable results in linear and nonlinear simulations up to 10 Hz.

The strain-stress relation, governing the non linear behaviour modeling and used at each time step, is based on the multishear mechanism model proposed by Towhata and Ishihara (1985). The multishear mechanism model is a plane strain formulation to simulate pore pressure generation in sands under cyclic loading and undrained conditions. After the work by Iai et al. (1990ab), the model was modified to account for the cyclic mobility and dilatancy of sands. However, in its basic form, this formulation models the soil nonlinearity without accounting for co-seismic water pore pressures. Bonilla (2000) added the damping control to the soil constitutive model.

The multiple mechanism model relates the effective stresses (σ') to the strain (ϵ) through the following incremental equation,

$$\{d\sigma'\} = [G] (\{d\epsilon\} - \{d\epsilon_p\}) \quad (1)$$

where the curly brackets represent the vector notation; $\{\epsilon_p\}$ is the volumetric strain produced by

the pore pressure, and $[G]$ is the tangent stiffness matrix. This matrix takes into account the volumetric and shear mechanisms, which are represented by the bulk and tangent shear moduli, respectively. The latter is idealized as a collection of I springs separated by $\Delta\theta = \pi / I$. Each spring follows the hyperbolic stress-strain model (Konder and Zelasko, 1963) and the generalized Masing rules for the hysteresis process. For more details on the nonlinear stress-strain rheology, the reader may see the papers by Iai et al. (1990ab) and Bonilla (2000).

Results from the models

The numerical results are analysed in terms of amplification functions $A(f)$, expressed by the spectral ratio among the superficial receivers and the reference total wavefield at the outcropping bedrock, as well as in terms of maximum shear strains (MSS) distributions along the vertical columns (for 1D models) or along the cross sections (for 2D models). Moreover, a comparison among the computed MSS and the γ_v is used to evaluate the representativeness of the rheological assumption (i.e. of viscoelastic equivalent linear and nonlinear elasto-plastic cyclic model).

Results from 1D numerical models

The 1D numerical models performed on the 48 soil columns by the use of EERA (equivalent linear) and SWAP_3C (nonlinear) codes pointed out that the first mode of resonance for all the columns is close to 1Hz with $A(f)$ values generally almost equal to 2. In several cases, depending on specific stratigraphical situations, other modes of resonance result at frequencies varying from 2 up to 5 Hz with $A(f)$ values up to 5, as in the case of the columns 11D, 11E and 5B.

The MSS computed through the nonlinear model (SWAP_3C) represents the octahedral shear strain; it takes into account the effects due to the 3D rheology and is generally higher than the

MSS computed through the equivalent linear model (EERA), see (Fig.8). Nevertheless this result depends at the same time on the various rheologies (equivalent linear and cyclic nonlinear) and on the number of components of the seismic input (i.e. 3 components for SWAP and 1 component for EERA). To evidence the role of the cyclic nonlinear rheology with respect to the equivalent linear one, a comparison of the computed MSS by EERA and SWAP considering one input component only is displayed in Fig. 8. As it results from this comparison, the MSS computed by SWAP generally exceed the ones computed by EERA.

The MSS resulting for the C layers are always higher than the ones measured in the other soil layers; moreover, they result more concentrated where the C layer is thinner, i.e. it results boxed within stiffer layers such as D1, B and G. Based on these outputs and considering the largest presence of the C layer when compared to the other ones within the alluvial deposits, this study was mostly focused on the behaviour of such a clayey layer within the alluvial fill. By analysing the MSS distribution along each selected soil column and within the C layers it results that: i) the highest values are generally located at the bottom of the layer (Fig.8), ii) the MSS increase with decreasing C layer thickness at the same depth (compare columns 7C and 8E in Fig.8); iii) the MSS values increase with depth for the same thickness of the stratum (see columns 7B and 8E in Fig.8) and iv) the MSS generally exceed the γ_v of the C layer (Figs. 8, 9).

In particular, Fig.9 shows that the exceedance of the γ_v threshold (expressed through the MSS/ γ_v ratio also considering the related standard deviation) is independent of the thickness of the C layer and the assumed rheology (i.e. EERA vs. SWAP)

These results highlight that both the layer thickness and the layer stratigraphical position along the soil column control the resulting MSS.

Results from 2D numerical models

The 2D models along the 4 selected sections (1, 6, 7 and 11) confirmed that the 1Hz frequency

is amplified all along the models with $A(f)$ values up to 4 (Figs.10,11,12,13); nevertheless significant amplifications result at higher frequencies (up to 8Hz). Along each section, 1D transfer functions were computed by discretizing the numerical domain in 5 m-spaced soil columns and by assuming a viscoelastic rheological model; the so obtained $A(f)$ values were reported in a unique plot as a function of the distance along the section (Figs.10b,11b,12b,13b). The computed 1D $A(f)$ functions were compared with the $A(f)$ functions obtained by the 2D viscoelastic modelling: such a comparison reveals a significant difference in the distribution of the amplification effects (Figs. 10b,c; 11b,c; 12b,c; 13b,c). In correspondence with lateral contact between stratigraphic layers characterised by high impedance contrasts (i.e. $\Delta V_s > 200$ m/s) the $A(f)$ functions do not appear as continuous since they are perturbed by interference fringes (Fig. 10c, 11c, 12c, 13c). The effects of nonlinearity are not negligible in terms of $A(f)$ distributions since they generally induce a reduction of the fundamental frequencies of about 0.5 Hz (Fig. 10d, 11d, 12d, 13d). Nonlinearity is also relevant for the interference fringes since they are significantly reduced and the basin effects related to the lateral heterogeneities correspond to $A(f)$ values lower than 2.

The resulting MSS distributions point out that for the same lithotechnical unit the maximum values result at the base of the alluvial body (Fig. 14). In particular, with reference to the C layer, a significant increase of the MSS values results for decreasing thickness of the layer itself and for a vertical confinement of thin layers between stiffer layers. This is particularly obvious around the central portion of the section 1 where the C layer is vertically confined between two layers D1 at a depth of about 35 m b.g.l..

As it results from the 2D numerical modeling the MSS generally exceed the γ_v threshold within the C layer (Fig.14); the percentage of exceedance is of the same order as for the 1D models (Fig.9, 14). Higher percentage values of exceedance are obtained where the C layer is thinner and vertically confined between stiffer deposits as for the MSS absolute values.

Discussion

Numerical results are analyzed in order to point out the effect of both vertical and lateral heterogeneities on the computed MSS. At this aim, a differential scheme is herein proposed: it is based on evaluating the difference, compared to a reference value, in some specific parameters influencing the MSS within the soil deposits.

Three main contributions are considered: the vertical heterogeneity related to the layering of the soil layers; the stratigraphic position of the layer, i.e. the depth measured from the ground layer; the lateral heterogeneities due to the contacts among soil deposits with significant impedance contrast, including the lateral contacts between soil and bedrock due to the 2D geometry of the river valley.

As previously discussed the present analysis is focused on the C layer only.

A first index (Shear Strain Concentration Index – SSCI) was introduced to quantify the concentration of MSS within the C layer in the form:

$$SSCI = \frac{\Delta\gamma}{\Delta h} = \frac{(\gamma_{max} - \gamma_{min})}{h_{max} - h_{min}} \quad (2)$$

where:

γ_{max} is the maximum shear strain within the C layer in the considered column; γ_{min} is the minimum shear strain within the C layer in the considered column; $(h_{max} - h_{min})$ is the difference between the two depths at which the minimum and maximum values of the shear strain are obtained within the C layer; this difference generally coincides with the thickness of the same layer (Fig. 15).

To subtract the effect due to the stratigraphic position of the layer (i.e. to its depth b.g.l.) the same index was computed for homogeneous reference columns only constituted by sands or clays over a stiff gravel layer representing the seismic bedrock. Eighteen reference columns were constructed by considering 2 soil compositions (sandy and clayey) and 9 thicknesses (i.e.

varying from 50 up to 70 m) to be representative for the different cases encountered in the modeled soil columns.

A differential index was defined in the form:

$$\Delta\Gamma = SSCI - SSCI_{ref} \quad (3)$$

where $SSCI$ is the shear strain concentration index for the C layer in each considered column and the $SSCI_{ref}$ is the one defined for the specific reference column.

The $\Delta\Gamma$ index reveals the effect due to vertical heterogeneity only, by excluding the effect due to the depth of the layer in the soil column; as it is shown by the graphs in Fig.16 a good correlation exists between the thickness of the C layer and the $\Delta\Gamma$ computed averaging all the values corresponding to the outputs of the soil columns characterized by the same thickness of the C layer. Such a correlation results for both the EERA and the SWAP_3C models (Fig.16a,b) and demonstrates that as the soil column heterogeneity increases (i.e. the C layer thickness is lower than 10 m which corresponds to almost 20% of the entire soil column) the average $\Delta\Gamma$ increases as well as the related standard deviation. As it results from these outputs, at an increasing vertical heterogeneity of the soil column corresponds a lower reliability of the shear strain prevision within the C layer, as it is strongly affected by the soil column stratigraphy, i.e. by the soil layering.

A similar analysis was carried out for the 2D modeling (Fig.16c); also in this case, the effect due to the vertical heterogeneity was analyzed by using the $\Delta\Gamma$ index. At this aim, 17 soil columns were extracted from the 4 modeled cross sections in correspondence to the same soil columns among the 48 considered ones, that are distributed along these sections. Also in this case, a good correlation exists between the thickness of the C layer and the $\Delta\Gamma$ computed averaging all values corresponding to the outputs of soil columns extracted along the sections and characterized by the same C layer thickness. Similarly to results obtained by the 1D models, the resulting $\Delta\Gamma$ distribution shows that the reliability of the shear strain prevision within the C

layer is strongly affected by the soil column stratigraphy as the computed standard deviation has a very sharp increase in the cases of C layer thickness lower than 10m.

In order to evaluate the effects of the horizontal heterogeneities, i.e. due to the lateral contacts among the soil layers as well as between the soil deposit and the bedrock, another differential index was introduced by subtracting the $\Delta\Gamma$ from 1D to the one from 2D model in the form:

$$\Delta\Gamma_{1D_2D} = | \Delta\Gamma_{1D} - \Delta\Gamma_{2D} | \quad (4)$$

As $\Delta\Gamma$ already subtracts the effect due to the stratigraphic position of the C layer with respect to its depth in the soil column, the $\Delta\Gamma_{1D_2D}$ index only takes into account the role of lateral heterogeneities in the computed MSS. To allow a comparison with the 2D modeling results and to better constrain the results expressed by $\Delta\Gamma_{1D_2D}$ index, the $\Delta\Gamma_{1D}$ was computed from the 1D models performed by the SWAP_3C code but using one ground motion component only.

A sensitivity analysis was performed by correlating the $\Delta\Gamma_{1D_2D}$ values and the distance (ΔX) measured from each considered column to the closest lateral contact due to heterogeneities which are characterized by a $\Delta V_s > 200\text{m/s}$, these last ones including the basin seismic bedrock (Bard and Bouchon, 1985; Semblat et al., 2010). The obtained $\Delta\Gamma_{1D_2D}$ vs. ΔX distribution demonstrates that the $\Delta\Gamma_{1D_2D}$ index is suitable for revealing the effect of lateral heterogeneities since its value significantly increases for decreasing distances between the soil column and the closest lateral contact. In particular, for distances lower than 300 m the $\Delta\Gamma_{1D_2D}$ value sharply increases from 0.005 up to about 0.025 according to an exponential correlation function (Fig. 17a). A similar analysis was carried out by searching a correlation among the $\Delta\Gamma_{1D_2D}$ index and the angle of inclination of the buried slopes at the basin edges (i.e. measured from the ground surface to the top of the G layer which represents the local seismic bedrock) (Fig. 17b). In this case, the outputs only show a decreasing trend of $\Delta\Gamma_{1D_2D}$ values with increasing slope angle; nevertheless, a proper correlation does not result and also for small slope angle ($<10^\circ$) the $\Delta\Gamma_{1D_2D}$ values are not negligible. These results demonstrate the main role played by lateral

heterogeneities with respect to the slope angle in the MSS concentration within the clay C layer of the Tiber River alluvia at Rome historical center. They also highlight the relevance of 2D models in case of lateral heterogeneities, where the lateral contacts are closer than 300 m from the considered soil column. Heterogeneities inside the basin can as well lead to different 1D and 2D basin responses (e.g., $x=1600\text{m}$ in section 11).

Based on these results a zonation of the historical center of Rome is proposed by distinguishing the areas in which the 1D conditions appear suitable for the numerical computing of the MSS within the C layer and the areas in which 2D conditions are more appropriate (Fig. 18). To obtain such a map, the 3D engineering geology model of the alluvial fill was used for contouring the 300 m distance from the C layer and the high-impedance lateral contacts as this distance seems suitable for assuming 1D instead of 2D numerical modeling conditions. This zonation shows that 1D effects are admissible for the Prati and P.zza Mancini quarters, while 2D conditions are generally more relevant for Rome historical quarters of Via del Corso, P.zza Venezia and Isola Tiberina island. An exception to this is provided by the area of P.zza Navona where it results a local stratigraphic setting suitable for 1D conditions.

The spatial distribution of the MSS computed for the C layer in the Rome historical center is also derived by the 1D or the 2D models depending on the more suitable resulting conditions; such a map represents a synthetic output which restitutes the shear strains expected for the maximum expected earthquake scenario within the clay deposits of the Tiber River in the Rome historical center. The relevance of the derived MSS distribution regards the possible interaction in case of ground motion of the building foundations and the infrastructures (such as pipelines, tunnels, tube-lines) with the highest deformability layers of the Rome subsoil that are generally encountered within the first 30 m b.g.l.. These outputs could be relevant for the design of seismic reinforcement also in case of monumental buildings or for new construction design.

Based on the transfer function measured by Caserta et al. (2013) at the Valco S. Paolo vertical accelerometric array, a 1D seismic response was observed for the site. In this case, the lateral

heterogeneities due to high-impedance contrast are localized at a distance higher than 300 m (Bozzano et al., 2008), i.e. in agreement with the correlation reported in Fig.17a the expected $\Delta\Gamma_{1D_2D}$ value is indeed suitable to a 1D strain effect.

It is worth noticing that, as it results from both the 1D and the 2D numerical models, the MSS/γ_v ratio distributions indicate that in several cases the γ_v threshold is exceeded more than one order of magnitude. Although the shaking conditions considered herein correspond to a very severe earthquake scenario for the city of Rome (i.e. the computed MSS are the maximum expected for a 10% of PGA exceedance in 50 years), a kind of criticism remains in the relevancy of the dynamic parameters resulting from resonant column tests (that generally provide the available dynamic parameters used for numerical modeling as in this study). This is particularly true under strictly nonlinear conditions (i.e. by considering strong motion effects), that imply a significant increase of the pore water pressures, and in case of heterogeneous deposits which not necessarily respect plane-parallel layering conditions. Another source of uncertainty is the variability of the reference input ground motion which could be addressed by further details in a more specific study.

Conclusions

This study was focused on the effects of earthquake shaking on shear strains by taking into account the effect of vertical and lateral heterogeneities due to the contacts among different soils within an alluvial fill deposit.

At this aim, the Rome historical center was selected as case study since a detailed 3D engineering-geology model of the subsoil is already available and a significant exposure exists due to the intense urbanization and to the monumental historical heritage of the area.

1D and 2D numerical models were focused on the evaluation of MSS within the clayey deposits

(i.e. ascribable to the lithotechnical layer C) which constitute the most part of the alluvial fill. Nonetheless, a kind of criticism remains on the suitability of properties derived from resonant column laboratory tests in case of high-strain level and heterogeneous soil conditions as the present results generally show a significant exceedance of the volume shear strain threshold γ_v in all the performed models.

To distinguish the effect due to both vertical heterogeneities (i.e. to the strata layering) and lateral heterogeneities, some specific indexes were defined. The SSCI index expresses the shear strain concentration within a specific layer of each soil column. The $\Delta\Gamma$ index subtracts the effect of the stratigraphic position of the considered soil layer since it compares the effect of a multilayered column with the one obtained along a homogeneous reference one. Finally, the $\Delta\Gamma_{1D_2D}$ evidences the effect due to the lateral heterogeneities; the responsiveness of this index to the distance of a soil column from the closest lateral contact with a high impedance contrast demonstrated its reliability and pointed out the dependence of the soil column position along a specific cross section to assume 2D or 1D conditions for numerically computing the expected MSS.

The $\Delta\Gamma_{1D_2D}$ was used for a zonation of the MSS in clay layer C of Rome historical center in terms of suitable areas for 1D or 2D numerical models. The present approach also provides useful indications for selecting the most suitable numerical approaches in the frame of seismic microzonation studies that, for the specific case of Rome, were not yet carried out.

This study shows the relevance of 2D models to provide expected values of MSS in case of soil deposits characterized by lateral heterogeneities; the obtained findings also point out that the role of heterogeneities is more relevant with respect to the shape of the valley bedrock, since the numerically computed MSS correlates well with the distance to the lateral contact while, conversely, no significant correlation exists with the angle of inclination of the buried slopes.

These obtained results encourage to improve the quality of the MSS evaluation within soil deposits under severe earthquake scenarios in urban areas, as they can interact with structure

foundations or infrastructures.

Data and Resources

The web-site of the Italian national project UHS INGV, Central Italy was visited at the web-site <http://esse1.mi.ingv.it/> (last accessed December 2013). For selecting the reference input the European Strong-motion Database (ESD) was visited at the web-site http://www.isesd.hi.is/ESD_Local/frameset.htm (last accessed July 2012).

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References

- Assimaki, D., Gazetas, G., and E. Kausel (2005). Effects of Local Soil Conditions on the Topographic Aggravation of Seismic Motion: Parametric Investigation and Recorded Field Evidence from the 1999 Athens Earthquake, *Bul Seism Soc Am*, **95**(3), 1059-1089.
- Athanasopoulos, G.A., Pelekis, P.C., and E.A. Leonidou (1999). Effects of surface topography on seismic ground response in the Egion (Greece) 15 June 1995 earthquake, *Soil Dynamics and*

607 *Earthquake Engineering*, **18**, 135-149.

608 Bakavoli, M.K., and E. Hagshenas (2010). Experimental and numerical study of topographic site
609 effect on a hill near Tehran, Proc. *Fifth International Conference of Recent Advances in*
610 *Geotechnical Earthquake Engineering and Soil Dynamics (May 24-29, S.Diego – California)*,
611 1-9.

612 Amato, A., Chiarabba, C., Cocco M., di Bona M., and M. G. Selvaggi (1994). The 1989– 1990
613 seismic swarm in the Alban Hills volcanic area, central Italy, *J. Volcanol. Geotherm. Res.*, **61**,
614 225–237.

615 Ambrosini, S., Castenetto, S., Cevolan, F., Di Loreto, E., Funiciello, R., Liperi, L. and D. Molin
616 (1986). Risposta sismica dell’area urbana di Roma in occasione del terremoto del Fucino del 13
617 Gennaio 1915, *Memorie della Società Geologica Italiana*, **35**, 445-452.

618 Assimaki, D., and W. Li (2012). Site and ground motion-dependent nonlinear effects in
619 seismological model predictions. *Soil Dynamics and Earthquake Engineering*, **32**, 143-151.

620 Bard P.Y. and M. Bouchon (1980a). The seismic response of sediment-filled valleys. Part I. The
621 case of incident SH waves, *Bull. Seism. Soc. Am.*, **70**, 1263-1286.

622 Bard P.Y. and M. Bouchon (1980b). The seismic response of sediment-filled valleys. Part II. The
623 case of incident P and SV waves, *Bull. Seism. Soc. Am.*, **70**, 1921-1941.

624 Bard, P.Y. and M. Bouchon (1985). The two-dimensional resonance of sediment-filled valleys,
625 *Bull. Seism. Soc. Am.*, **75**, 519 - 541.

626 Bardet, J. P., Ichii, K., and C. H. Lin (2000). EERA: a computer program for equivalent-linear
627 earthquake site response analyses of layered soil deposits, *Report University of Southern*
628 *California, Department of Civil Engineering*.

629 Bardet, J. P., and T. Tobita (2001). NERA: A Computer Program for Nonlinear
630 Earthquake Site Response Analyses of Layered Soil Deposits,

631 *University of Southern California, California.*

632 Blumetti, A.M., Comerci, V., Di Manna, P., Guerrieri, L., and E. Vittori (2009). Geological effects
633 induced by the L'Aquila earthquake (6 April 2009, M_L=5.8) on the natural environment, *iSPra -*
634 *Dipartimento Difesa del Suolo - Servizio geologico d'italia, preliminary report, 38.*

635 Bonilla, F., Gélis, C., Giacomini, A.C, Lenti, L., Martino, S. and J.F. Semblat (2010).
636 Multidisciplinary study of seismic amplification in the historical center of Rome, Italy, *Proc.*
637 *5th Int. Conf. on Recent Advances in Geotech. Earthq. Engin. and Soil Dynamics, May 24-29*
638 *2010, San Diego, California.*

639 Bonilla, L.F., Tsuda, K., Pulido, N., Regnier, J. and A. Laurendeau (2011). Nonlinear site response
640 evidence of K-net and KiK-net records from the Mw 9 Tohoku earthquake. *Earth Planets*
641 *Space*, **58**, 785-789.

642 Bonilla, L. F., Liu, P. C., and S. Nielsen (2006). 1D and 2D linear and nonlinear site response in the
643 Grenoble area, *Proc. 3rd Int. Symp. on the Effects of Surface Geology on Seismic Motion*
644 *(ESG2006).*

645 Borchardt R. D. (1994). Estimates of site-dependent response spectra for design (methodology and
646 justification), *Earthq. Spectra*, **10**, 617–653.

647 Bouden-Romdhane N., Kham, M., Semblat, J.F. and P. Mechler, (2003). 1D and 2D response
648 analysis vs experimental data from Tunis city. Beşinci Ulusal Deprem Mühendisliği Konferansı,
649 26-30 Mayıs 2003, *Proc. 5th National Conference on Earthquake Engineering, 26-30 May*
650 *2003, Istanbul, Turkey, Paper No: AE-051.*

651 Bozzano, F., Andreucci, A., Gaeta, M., Salucci, R. and C. Rosa (2000). A geological model of the
652 buried Tiber River valley beneath the historical center of Rome, *Bull. Eng. Geol. Env.*, **59**, 1-21.

653 Bozzano, F., Bretschneider, A., Giacomini, A.C., Lenti, L., Martino, S., Scarascia Mugnozza, G.,
654 Stedile, L. and J.L. (2012). Undrained behaviour of the sandy-silty levels of the Tiber River

alluvial deposits in Rome (Italy), *Italian Journal of Engineering Geology and Environment*,
2(2002), 47-61.

Bozzano, F., Caserta, A., Govoni, A., Marra, F. and S. Martino (2008). Static and dynamic
characterization of alluvial deposits in the Tiber River Valley: new data for assessing potential
ground motion in the city of Rome, *Journal of Geophysical Research*, **113**, 1-21.

Bozzano, F., Funiciello, R., Gaeta, M., Marra, F., Rosa, C. and G. Valentini (1997). Recent alluvial
deposit in Rome (Italy): morpho-stratigrafic, mineralogical and geomechanical characterisation,
Proc. of the International Symposium of Engineering Geology and Environment, Publ 1, 1193-
1198.

Bozzano, F., Giacomini, A.C., Martino, S. and Corpo Nazionale Vigili del Fuoco (2011). Scenario di
danneggiamento indotto nella città di Roma dalla sequenza sismica aquilana del 2009, *Italian
Journal of Engineering Geology and Environment*, **2(2011)**, 5-22.

Campolunghi, M.P., Capelli, G., Funiciello, R. and M. Lanzini (2007). Geotechnical studies for
foundation settlement in Holocenic alluvial deposits in the City of Rome (Italy), *Engineering
Geology*, **89**, 9-35.

Caserta, A., Boore, D. M., Rovelli, A., Govoni, A., Marra, F., Della Monica, G. and E. Boschi
(2013). Ground Motions Recorded in Rome during the April 2009 L'Aquila Seismic Sequence:
Site Response and Comparison with Ground Motion Predictions Based on a Global Dataset,
Bull. Seism. Soc. Am., **103(3)**, 1860-1874.

Cipollari, P., Cosentino, D. and N. Perilli (1993). Analisi biostratigrafica dei depositi terrigeni a
ridosso della linea Olevano-Antrodoco, *Geologica Romana*, **29**, 495-513.

Corazza, A., Lanzini, M., Rosa, C. and R. Salucci (1999). Caratteri stratigrafici, idrogeologici e
geotecnici delle alluvioni tiberine del settore del centro storico di Roma, *Il Quaternario*, **12**,
215-235.

679 Di Giulio, G., Improta, L. , Calderoni, G. and A. Rovelli (2008). A study of the seismic response of
680 the A.city of Benevento (Southern Italy) through a combined analysis of seismological and
681 geological data. *Engineering Geology*, **97**, 146–170.

682 Donati, S., Cifelli, F. and F. Funiciello (2008). Indagini macrosismiche ad alta densità per lo studio
683 del risentimento sismico nella città di Roma, *Memorie Descrittive Carta Geologica d'Italia*, **80**,
684 3-13.

685 Donati, S., Funiciello, R. and A. Rovelli (1999). Seismic response in archaeological areas: the
686 Case-History of Rome, *Jour. Appl. Geophys.*, **41**, 229 239.

687 Fäh, D., C. Iodice, P. Suhadolc, and G. F. Panza (1993). A new method for the realistic estimation
688 of seismic ground motion in megacities: The Case of Rome, *Earthquake Spectra*, **9**, 643– 668.

689 Gélis C., and L.F. Bonilla (2012). 2D P-SV numerical study of soil-source interaction in a non-
690 linear basin, *Geophys. J. Int.*, **191**, 1374–1390.

691 Gélis, C. and L.F. Bonilla (2014). Influence of a sedimentary basin infilling description of the 2D P-
692 SV wave propagation using linear and nonlinear constitutive models, *Geophys. J. Int.*, **198**,
693 1684–1700.

694 Gélis, C., Leparoux, D., Virieux, J., Bitri, A., Operto, S. And G. Grandjean G. (2005). Numerical
695 modeling of surface waves over shallow cavities, *Journal of Environmental & Engineering*
696 *Geophysics*, **10(2)**, 111-121.

697 Iai, S., Matsunaga, Y., and T. Kameoka (1990-a). Strain space plasticity model for cyclic mobility,
698 *Report of the Port and harbour Research Institute*, 29(4).

699 Iai, S., Matsunaga, Y. and T. Kameoka (1990-b). Parameter identification for a cyclic mobility
700 model. *Report of the Port and harbour Research Institute*, 29(4), 57-83.

701 Iwan, W. D. (1967). On a class of models for the yielding behavior of continuous and composite
702 systems. *Journal of Applied Mechanics*, **34**, 612.

703 Joyner A. L., Kornberg T., Coleman K. G., Cox D. R., and G. R. Martin (1985). Expression during
 704 embryogenesis of a mouse gene with sequence homology to the *Drosophila engrailed* gene,
 705 *Cell*, **43(1)**, 29-37.

706 Joyner, W. B. and A. T. Chen (1975). Calculation of nonlinear ground response in earthquakes.
 707 *Bull. Seism. Soc. Am.*, **65(5)**, 1315-1336.

708 Kham, M., Semblat, J.F., Bard, P.Y., and P. Dangla (2006). Seismic site-city interaction: main
 709 governing phenomena through simplified numericla models. *Bull. Seism. Soc. Am.*, **96(5)**,
 710 1934-1951.

711 Karner D.B. and F. Marra (1998). Correlation of Fluviodeltaic Aggradational Sections with Glacial
 712 Climate History: A Revision of the Classical Pleistocene Stratigraphy of Rome, *Geol. Soc. Am.*
 713 *Bull.*, **110**, 748-758.

714 Karner, D.B. and Renne P.R. (1998). ⁴⁰Ar/³⁹Ar Geochronology of Roman Volcanic Province
 715 Tephra in the Tiber River Valley: Age Calibration of Middle Pleistocene Sea-Level Changes,
 716 *Bull. Seis. Soc. Am.*, **110**, 740-747.

717 Konder, R.L. and Zelasko J.S. (1963). A hyperbolic stress-strain formulation for sands, *Proc. of 2nd*
 718 *Pan American Conference on Soil Mechanics and Foundation Engineering, Brazil*, 289-324.

719 Lanzo, G. and F. Silvestri (1999). Risposta sismica locale: teoria ed esperienze, *Hevelius (Editors)*,
 720 *pp.* 159.

721 Lenti, L., Martino, S., Paciello, A., and G.S. Mugnozza (2009). Evidence of two-dimensional
 722 amplification effects in an alluvial valley (Valnerina, Italy) from velocimetric records and
 723 numerical models, *Bull. Seis. Soc. Am.*, **99(3)**, 1612-1635.

724 Semblat, J.F., Lokmane, N., Driad-Lebeau, L., and G. Bonnet (2010). Local amplification of deep
 725 mining induced vibrations part.2: simulation of ground motion in a coal basin. *Soil Dynamics*
 726 *and Earthquake Engineering*, **30**, 947-957.

727 Makra, K., Chávez-García, F. J., Raptakis, D. and K. Pitilakis (2005). Parametric analysis of the
728 seismic response of a 2D sedimentary valley: implications for code implementations of complex
729 site effects, *Soil Dynamics and Earthquake Engineering*, **25(4)**, 303-315.

730 Mancini, M., Moscatelli, M., Stigliano, F., Cavinato, G. P., Marini, M., Pagliaroli, A. and M.
731 Simionato (2013). Fluvial facies and stratigraphic architecture of Middle Pleistocene incised
732 valleys from the subsoil of Rome (Italy), *Journal of Mediterranean Earth Sciences*, **Special**
733 **Issue**, 89-93.

734 Marra, F., Florindo, F. and D.B. Karner (1998). Paleomagnetism and geochronology of early
735 Middle Pleistocene depositional sequences near Rome: comparison with the deep sea $\delta^{18}\text{O}$
736 climate record, *Earth and Planetary Science Letters*, **159**, 147-164.

737 Marra, F., Rosa C., De Rita, D. and R. Funiciello (1998). Stratigraphic and tectonic features of the
738 middle Pleistocene sedimentary and volcanic deposits in the area of Rome (Italy), *Quaternary*
739 *International*, **47-48**, 51-63.

740 Milli, S., D'Ambrogi, C., Bellotti, P., Calderoni, G., Carboni, M.G., Celant, A., Di Bella, L., Di
741 Rita, F., Frezza, V., Magri, D., Pichezzi, R.M. and V. Ricci (2013). The transition from
742 wavedominated estuary to wave-dominated delta: The Late Quaternary stratigraphic
743 architecture of Tiber River deltaic succession (Italy), *Sedimentary Geology*, **284-285**, 159-180.

744 Molin, D., and E. Guidoboni (1989). Effetto fonti effetto monumenti a Roma: i terremoti
745 dall'antichità ad oggi, "I terremoti prima del mille in Italia e nell'Area mediterranea", Ed. E.
746 Guidoboni, Bologna, 194-223.

747 Mozco, P., and P. Y. Bard (1993). Wave diffraction, amplification and differential motion near
748 strong lateral discontinuities, *Bull. Seismol. Soc. Am.*, **83(1)**, 85-106.

749 Olsen K. B., Akinici A., Rovelli A., Marra F., and L. Malagnini (2006). 3D ground-motion
750 estimation in Rome, Italy, *Bull. Seismol. Soc. Am.*, **96(1)**, 133-146.

751 Panza, G.F., Alvarez, L., Aoudia, A., Ayadi, A., Benhallou, H., Benouar, D., Bus, Z., Chen, Y.,
 752 Cioflan, C., Ding, Z., El-Sayed, A., Garcia, J., Garofalo, B., Gorshkov, A., Gribovszki, K.,
 753 Harbi, A., Hatzidimitriou, P., Herak, M., Kouteva, M., Kuzntzov, I., Lokmer, I., Maouche, S.,
 754 Marmureanu, G., Matova, M., Natale, M., Nunziata, C., Parvez, I., Pasckaleva, I., Pico, R.,
 755 Radulian, M., Romanelli, F., Soloviev, A., Suhadolc, P., Szeidovitz, G., Triantafyllidis, P., and
 756 F. Vaccari (2004). Realistic modeling of seismic input for megacities and large urban areas, *J.*
 757 *Tech. Environ. Geol.*, **1**, 6-42.

758 Pergalani, F., Compagnoni, M. and V. Petrini, V. (2008). Evaluation of site effects using numerical
 759 analyses in Celano (Italy) finalized to seismic risk assessment, *Soil Dynamics and Earthquake*
 760 *Engineering*, **28(12)**, 964-977.

761 Pergalani, F., Romeo, R., Luzi, L., Petrini, V., Pugliese, A. And T. Sanò, T. (1999). Seismic
 762 microzoning of the area struck by Umbria–Marche (Central Italy) Ms 5.9 earthquake of 26
 763 September 1997, *Soil Dynamics and Earthquake Engineering*, **18(4)**, 279-296.

764 Peyrusse F., Glinsky N., Gelis C. and S. Lanteri (2014). A nodal discontinuous Galerkin method for
 765 site effects assessment in viscoelastic media - verification and validation in the Nice basin.
 766 *Geophys. J. Int.*, **199**, 315–334

767 Raspa, G., Moscatelli, M., Stigliano, F., Patera, A., Marconi, F., Folle, D., Vallone, R., Mancini,
 768 M., Cavinato, G. P., Milli, S., Coimbra, J.F. and L. Costa (2008). Geotechnical characterization
 769 of the upper Pleistocene-Holocene alluvial deposits of Roma (Italy) by means of multivariate
 770 geostatistics: Cross-validation results, *Engineering Geology*, **101**, 251-268.

771 Rassem, M., Ghobarah, A. and C. Heidebrecht (1997). Engineering perspective for the seismic site
 772 response of alluvial valleys, *Earthq. Eng. Struct. Dyn.*, **26**, 477–493.

773 Régnier, J., Cadet, H., Bonilla L.F., Bertrand, E., and J.F. Semblat (2013). Assessing nonlinear
 774 behavior of soils in seismic site response. statistical analysis on KiK-net strong-motion data.
 775 *Bull. Seismol. Soc. Am.*, **103(3)**, 1750-1770.

776 Rovelli, A., Caserta, A., L. Malagnini, and F. Marra (1994). Assessment of potential strong motions
777 in the city of Rome, *Annali di Geofisica*, **37**, 1745–1769.

778 Rovelli, A., Malagnini, L., Caserta, A. and F. Marra (1995). Using 1-D and 2-D modeling of ground
779 motion for seismic zonation criteria: results for the city of Rome, *Annali di Geofisica*, **38(5-6)**,
780 591-605.

781 Saenger, E. H., Gold, N. and S. A. Shapiro (2000). Modeling the propagation of elastic waves
782 using a modified finite-difference grid, *Wave motion*, **31(1)**, 77-92.

783 Santisi d'Avila, M. P., Lenti, L., and J.F. Semblat (2012). Modeling strong seismic ground motion:
784 three-dimensional loading path versus wavefield polarization, *Geophysical Journal*
785 *International*, **190(3)**, 1607-1624.

786 Santisi d'Avila, M. P., Semblat, J. F. and L. Lenti (2013). Strong Ground Motion in the 2011
787 Tohoku Earthquake: A One-Directional Three-Component Modeling, *Bull. Seismol. Soc. Am.*,
788 **103**, 1394-1410.

789 Segalman, D. J. and M. J. Starr (2008). Inversion of Masing models via continuous Iwan systems,
790 *International Journal of Non-Linear Mechanics*, **43(1)**, 74-80.

791 Semblat, J. F., Dangla, P., Kham, M. and A. M. Duval (2002-a). Seismic site effects for shallow and
792 deep alluvial basins: in-depth motion and focusing effect, *Soil Dynamics and Earthquake*
793 *Engineering*, **22(9)**, 849-854.

794 Semblat, J.F., Duval, A.M. and P. Dangla (2000). Numerical analysis of seismic wave amplification
795 in Nice (France) and comparisons with experiments, *Soil Dyn. Earthq. Eng.*, **19(5)**, 347–62.

796 Semblat, J. F., Duval, A.M. and P. Dangla (2002-b). Seismic site effects in a deep alluvial basin:
797 numerical analysis by the boundary element method, *Computers and Geotechnics*, **29(7)**, 573-
798 585.

799 Semblat, J.F., Kham, M., Parara, E., Bard, P.Y., Pitilakis, K., Makra, K. and D. Raptakis (2005).

800 Site effects: basin geometry vs soil layering, *Soil Dynamics and Earthquake Engineering*, **25(7-**
801 **10)**, 529-538.

802 Semblat, J.F., Kham, M., and P.Y. Bard (2008). Seismic-wave propagation in alluvial basins and
803 influence of site-city interaction. *Bull. Seismol. Soc. Am.*, **98(6)**, 2665-2678.

804 Semblat, J.F. and A. Pecker (2009). *Waves and vibrations in soils: Earthquake, traffic, shocks,*
805 *construction works*, IUSS Press, ISBN: 8861980309, 499 pp.

806 Sørensen, M.B., Oprsal, I., Bonnefoy-Claudet, S., Atakan, K., Mai, P. M., Pulido, N. and C.
807 Yalciner (2006). Local site effects in Ataköy, Istanbul, Turkey, due to a future large earthquake
808 in the Marmara Sea, *Geophysical Journal International*, **167(3)**, 1413-1424.

809 Tertulliani, A., Tosi, P. and V. De Rubeis (1996). Local seismicity in Rome (Italy): recent results
810 from macroseismic evidences, *Annali di Geofisica*, **39(6)**, 1235–1240.

811 Towhata I. and K. Ishiara (1985). Modeling Soil Behavior Under Principal Axes Rotation, *Proc. 5th*
812 *Fifth International Conference on Numerical Methods in Geomechanics, Nagoya*, 523-530.

813 Virieux J. (1986). P-SV wave propagation in heterogeneous media: Velocity-stress finite-difference
814 method, *Geophysics*, **51(4)**, 889-901.

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833 **Captions to figures**

834 Fig.1 – a) Location of the city of Rome respect to the central Apennines (modified from Cipollari et
835 al., 1993) the : 1) alluvial and coastal deposits; 2) volcanic deposits; 3) terrigenous flysch deposits;
836 4) limestones; 5) main thrust; 6) main fault; 7) epicentral location of the 1915 Avezzano and of the
837 2009 L’Aquila earthquakes. b) satellite GoogleEarth view the Rome historical center; the locations
838 of the considered soil columns and sections are also shown (the 2D modeled sections are indicated
839 by a circled number).

840 Fig.2 – Borehole stratigraphic log showing the main lithotechnical units that were distinguished in
841 the Tiber River alluvial deposits at Rome historical center.

842 Fig.3 – a) Rheological and velocity model assumed for the subsoil of the Rome historical center, (*)
843 dynamic properties available so far from specific laboratory tests; b) normalized shear modulus

844 (G/G₀) and damping (D) vs. shear strain (γ) used in the numerical models and referred to each
845 lithotechnical unit.

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847 example of geological cross section extracted from the 3D model and; c) smoothing of the
848 geological cross-section for the numerical models.

849 Fig.5 – Percentage distribution of the soil layers (a) and percentage distribution of the clayey C
850 layer thickness (b) within the here considered 48 soil columns of the Tiber River alluvial deposits at
851 Rome historical center.

852 Fig.6 – Reference 3-component input used for the numerical modeling (by Guido Martini, ENEA –
853 Italy): timehistories (left column) and Fast Fourier Transform (right column) of the horizontal (up
854 and middle) and vertical (down) components of the input.

855 Fig.7 – Engineering-geological cross sections along the traces 1, 6, 7 and 11 (see Fig.1 for location)
856 used for the performed 2D numerical models. The 17 soil columns considered for computing the
857 $\Delta\Gamma_{1D_2D}$ index are also shown (see also Fig.1 for location).

858 Fig.8 – MSS distribution along some of the 48 modeled soil columns (see Fig.1 for location) by the
859 codes EERA and SWAP; in the case of SWAP the MSS distribution for both the 1-component input
860 (SWAP_1C) and for the 3-component input (SWAP_3C) are distinguished.

861 Fig.9 – Average MSS/ γ_v vs. the C layer thickness distributions (+/- standard deviation, dashed lines)
862 in the case of: a) EERA (1-component input); b) SWAP (3-component input). The labels close to
863 the black circles indicate the number of cases considered for the mean.

864 Fig.10 – Outputs of the 2D numerical model performed along section 1 of Fig.7: a) V_s value
865 distribution in the numerical domain; b) A(f) function from the 1D viscoelastic solution; c) A(f)

866 function from the 2D viscoelastic solution; d) A(f) function from the 2D viscoplastic solution. The
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868 Fig.11 – Outputs of the 2D numerical model performed along section 6 of Fig.7: a) Vs value
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872 Fig.12 – Outputs of the 2D numerical model performed along section 7 of Fig.7: a) Vs value
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876 Fig.13 – Outputs of the 2D numerical model performed along section 11 of Fig.7: a) Vs value
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880 Fig.14 – MSS/ γ_v ratio distributions resulting by the 2D numerical models for section 1 (a), 6 (b), 7
881 (c) and 11 (d); the MSS distributions within the models are also reported.

882 Fig.15 – Sketch that illustrates the $\Delta\Gamma$ index obtained by subtracting the SSCI index computed for
883 the C layer in a general column to the same index computed for the corresponding reference
884 column.

885 Fig.16 - $\Delta\Gamma$ index distributions vs. C layer thickness as they result from the EERA, SWAP_3C (for
886 a 3-component input) and 2D numerical models. The outputs are referred to the 48 soil columns of
887 Fig.1 for the 1D models and to the 17 soil columns of Fig.7 for the 2D models. The labels close to
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889 Fig,17 – a) $\Delta\Gamma_{1D_2D}$ index distributions vs. the maximum distance of the C layer from the closest
890 high-impedance ($\Delta V_s > 200$ m/s) lateral contact (ΔX) and b) $\Delta\Gamma_{1D_2D}$ index distributions vs. the
891 inclination angles of the slope buried below the alluvial deposits in the Tiber River valley at Rome
892 historical center.

893 Fig.18 – GoogleEarth satellite view of the Rome historical center in which the Tiber River alluvial
894 deposits are bounded by a bold white lines and the zones suitable for 1D (areas with the white lines)
895 and 2D (areas without lines) shear strain effects are mapped; MSS values expected in the C layer
896 for the 475-years earthquake scenario are also reported.

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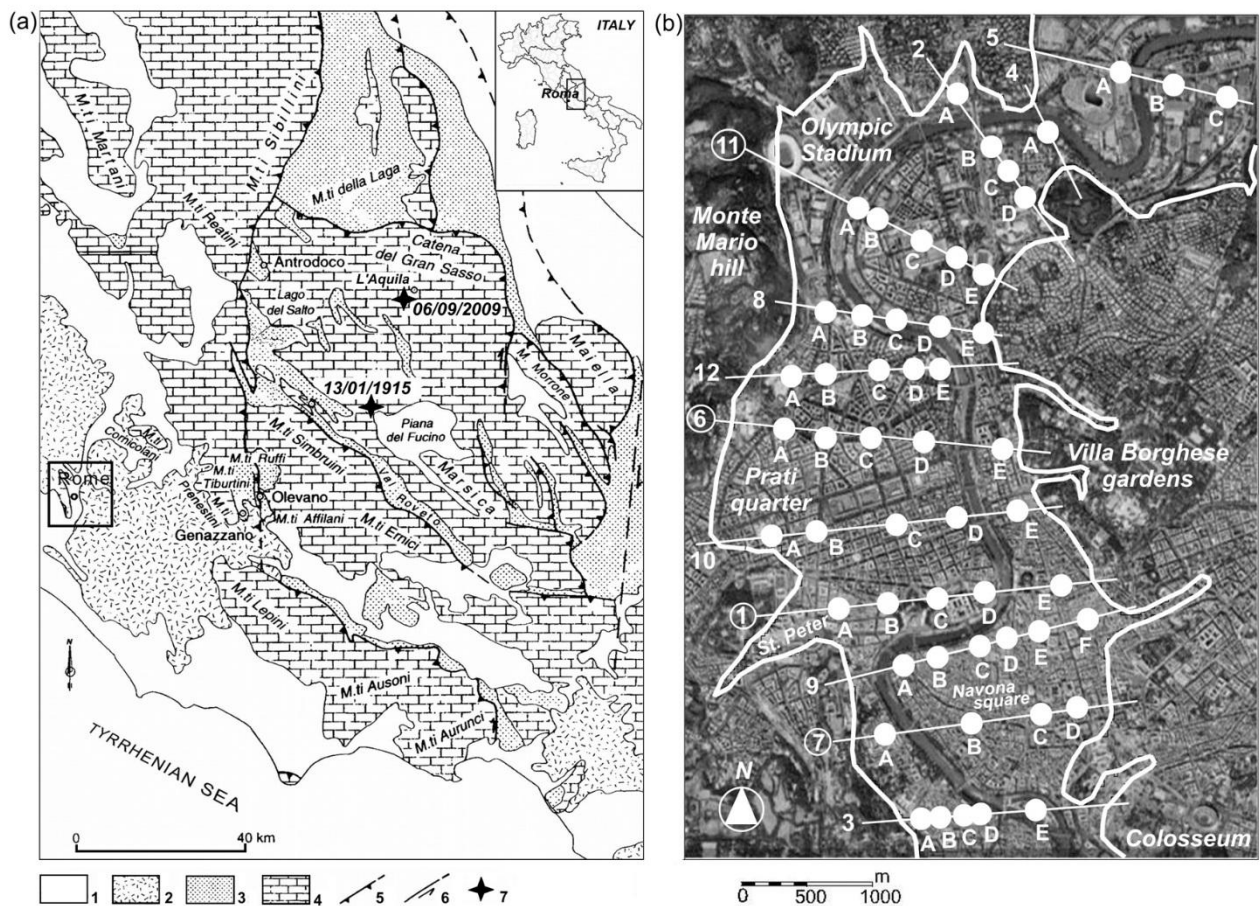
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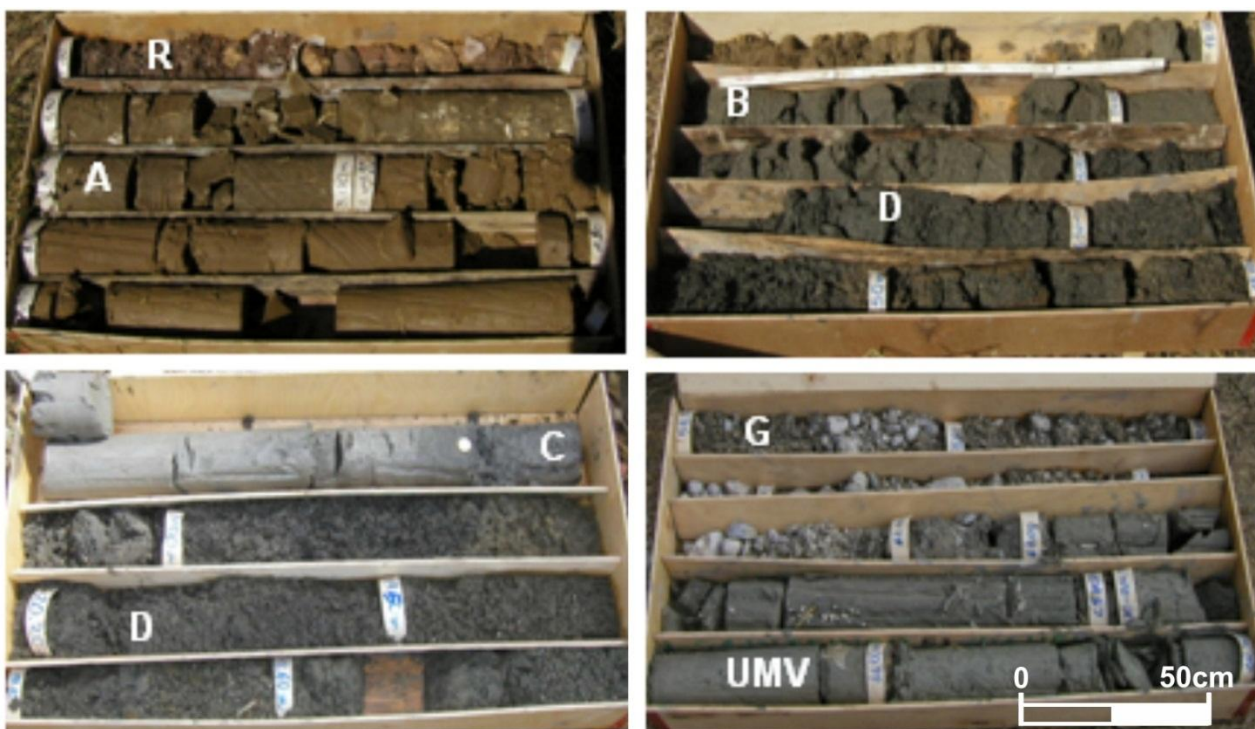
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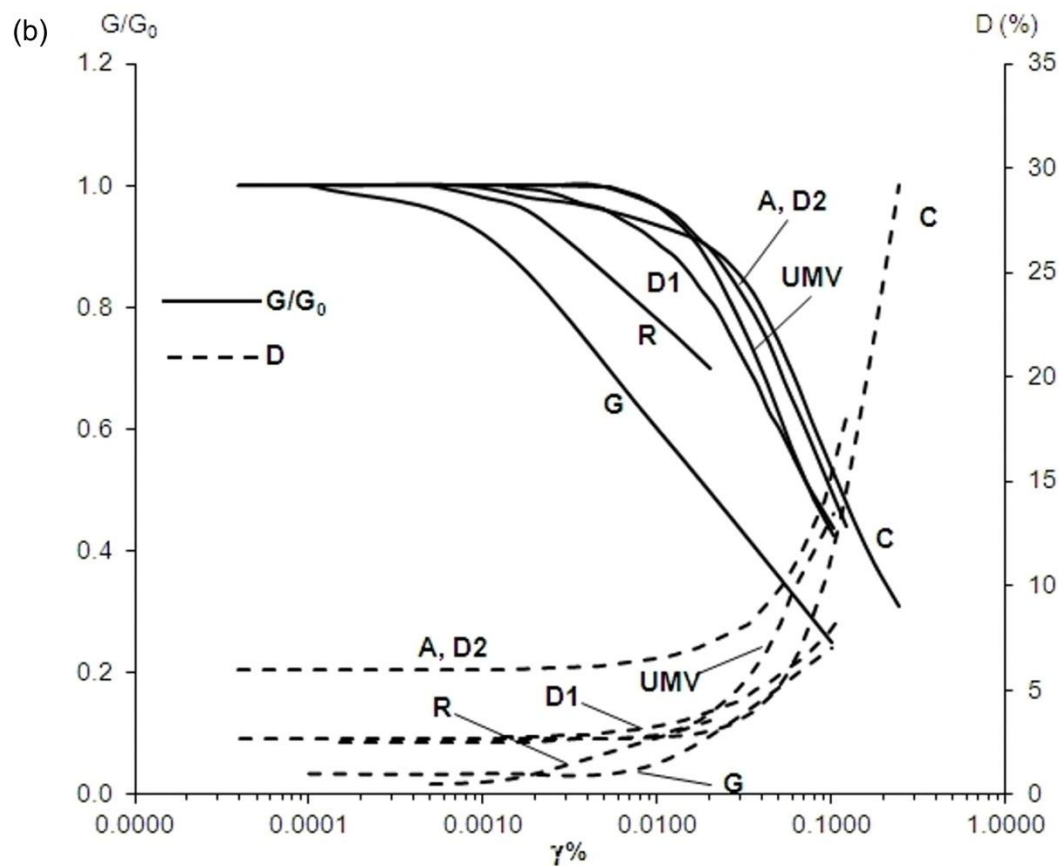
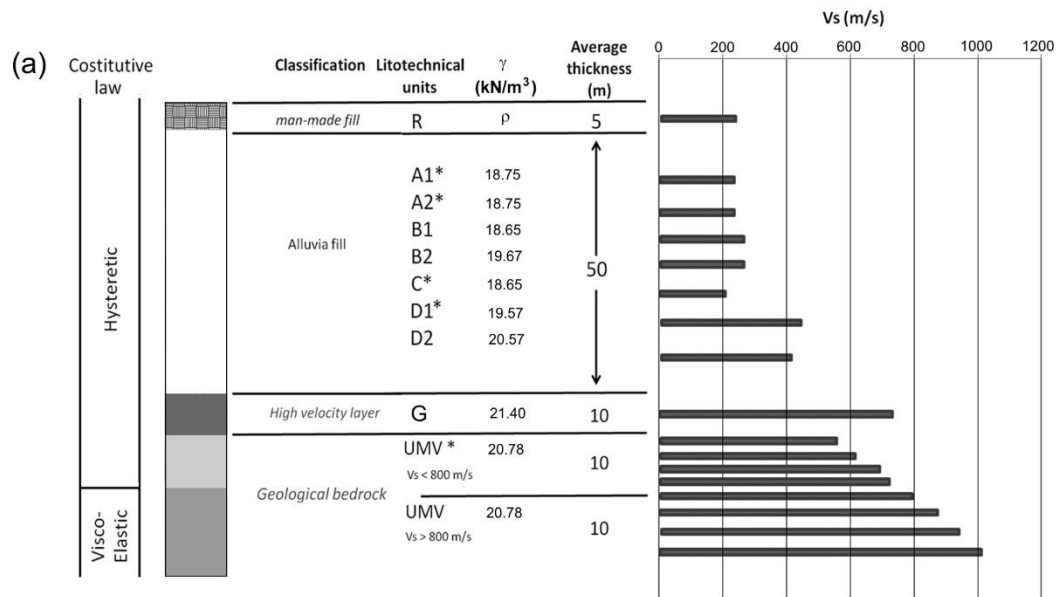
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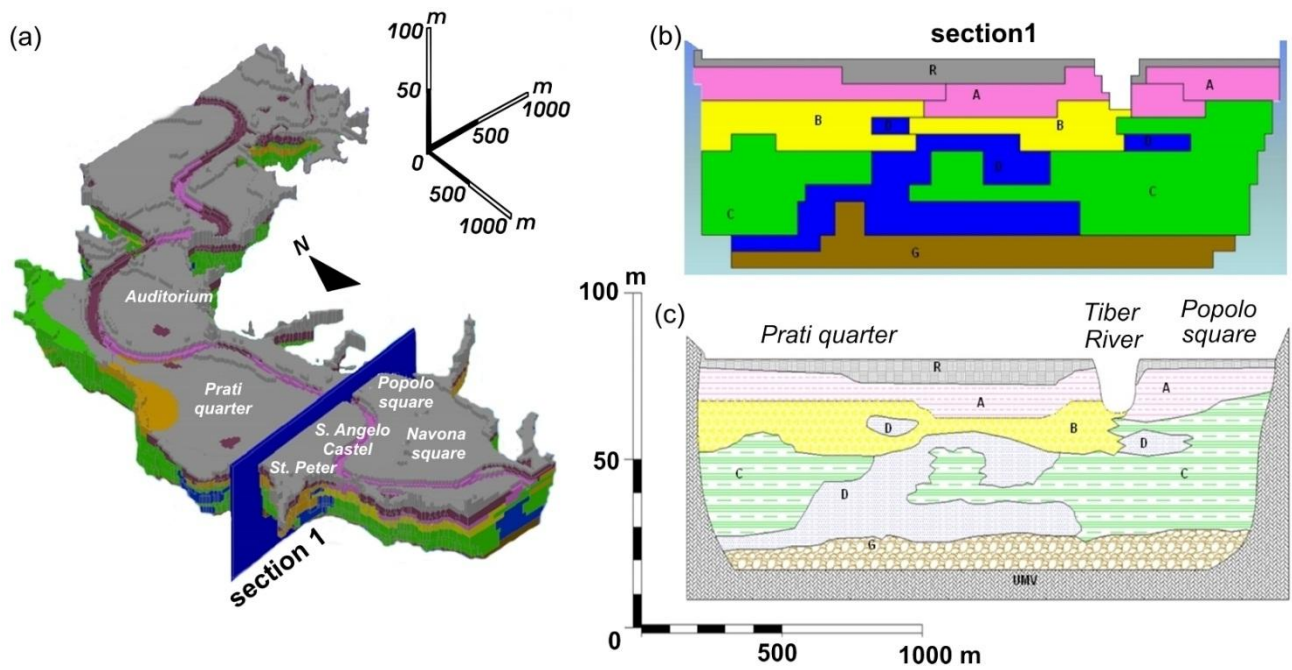
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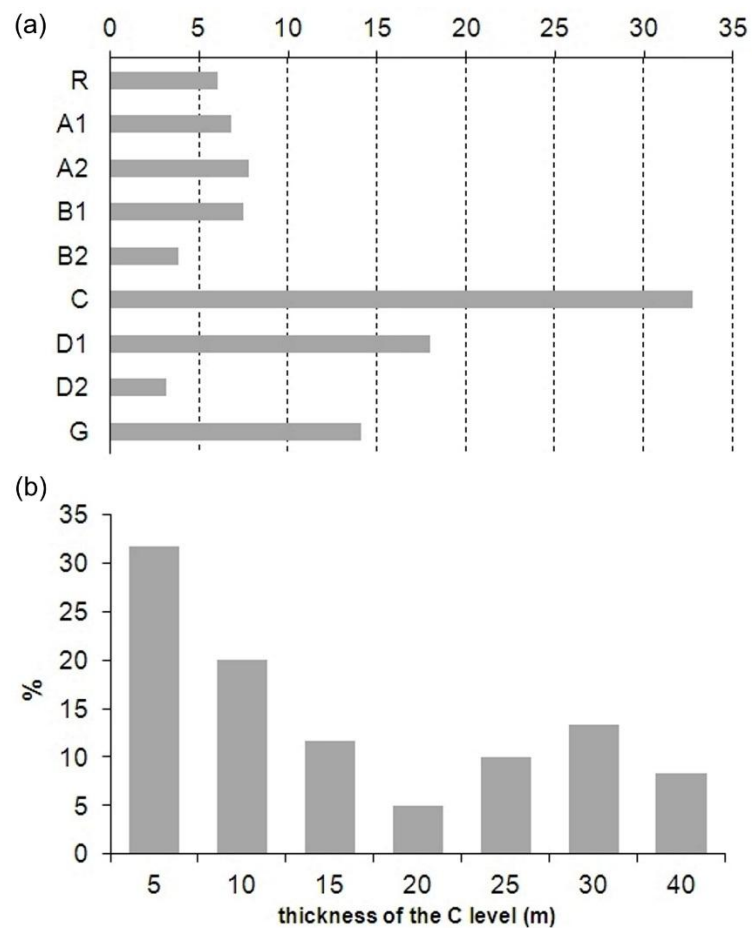
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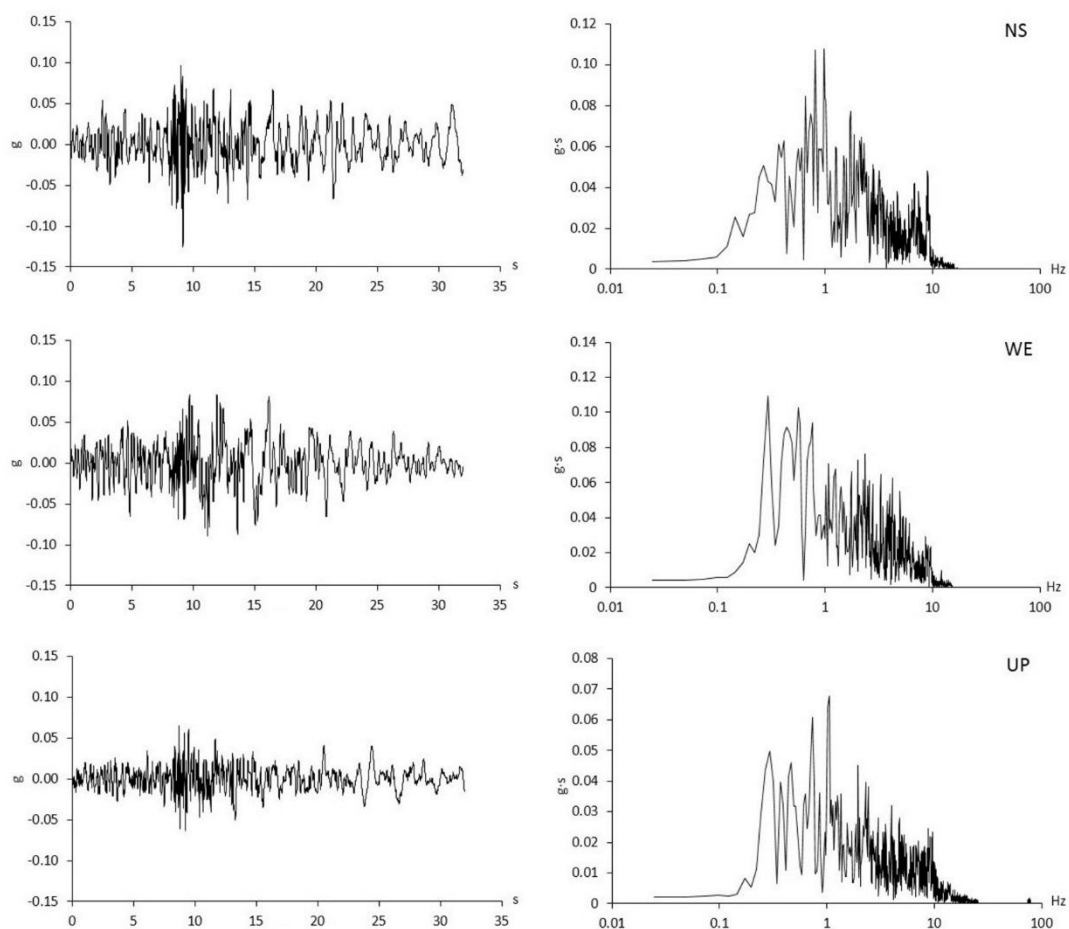
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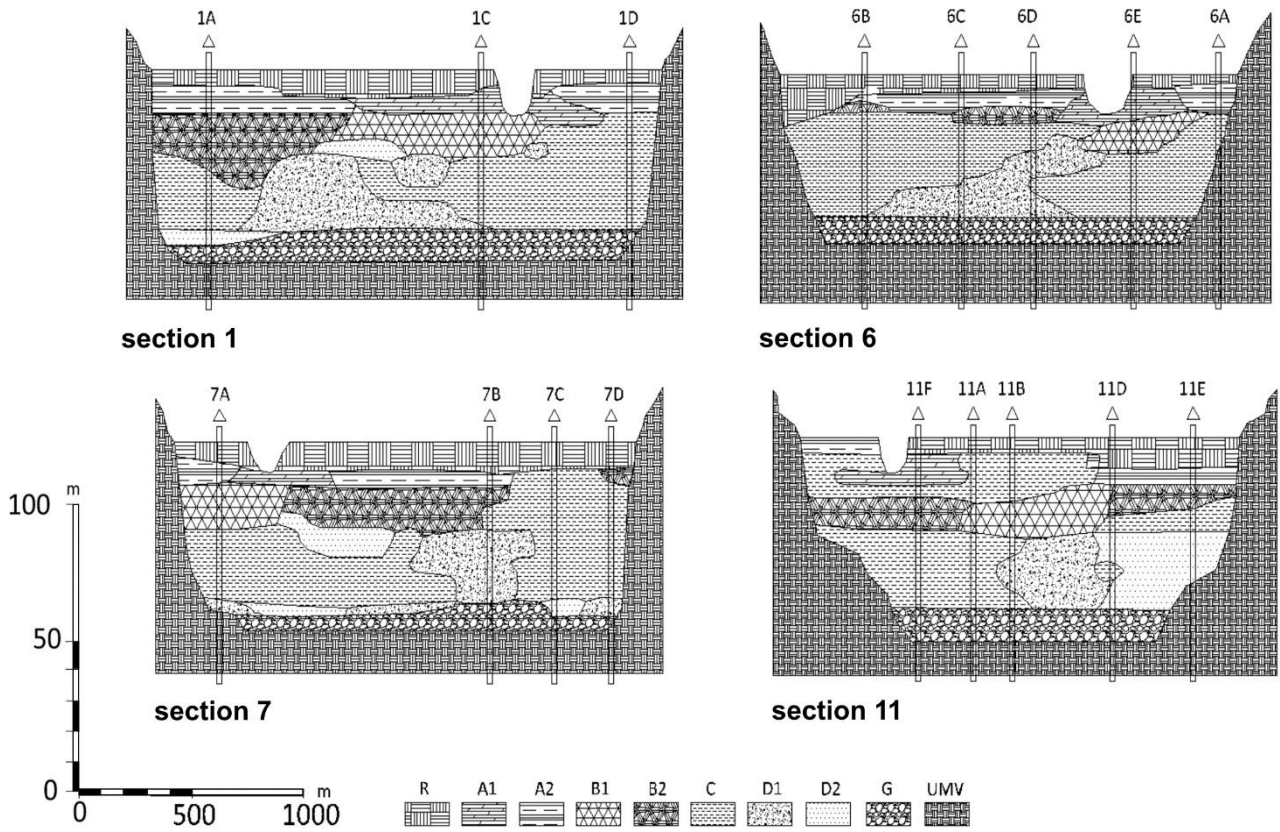
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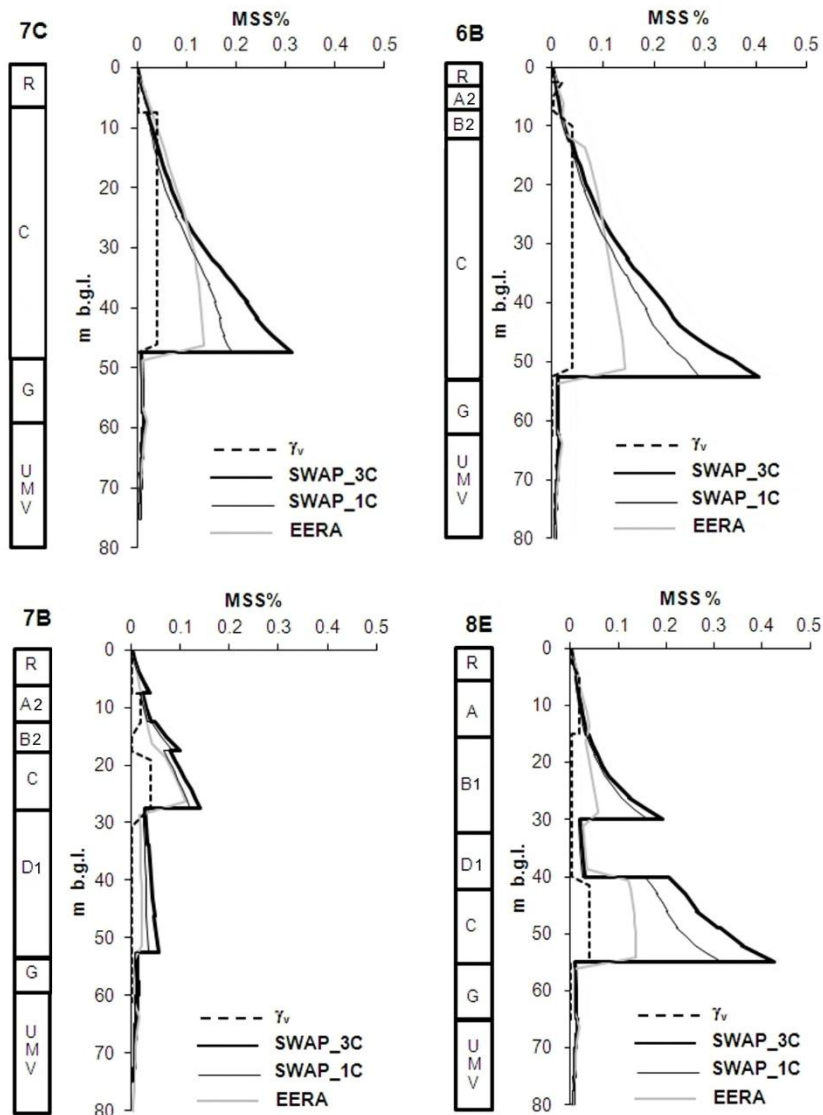
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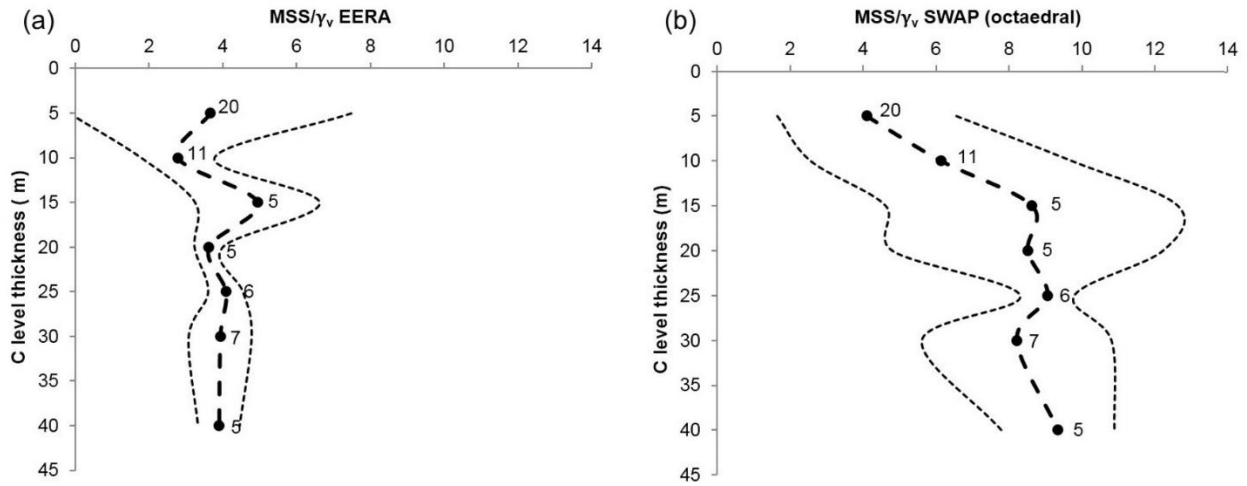
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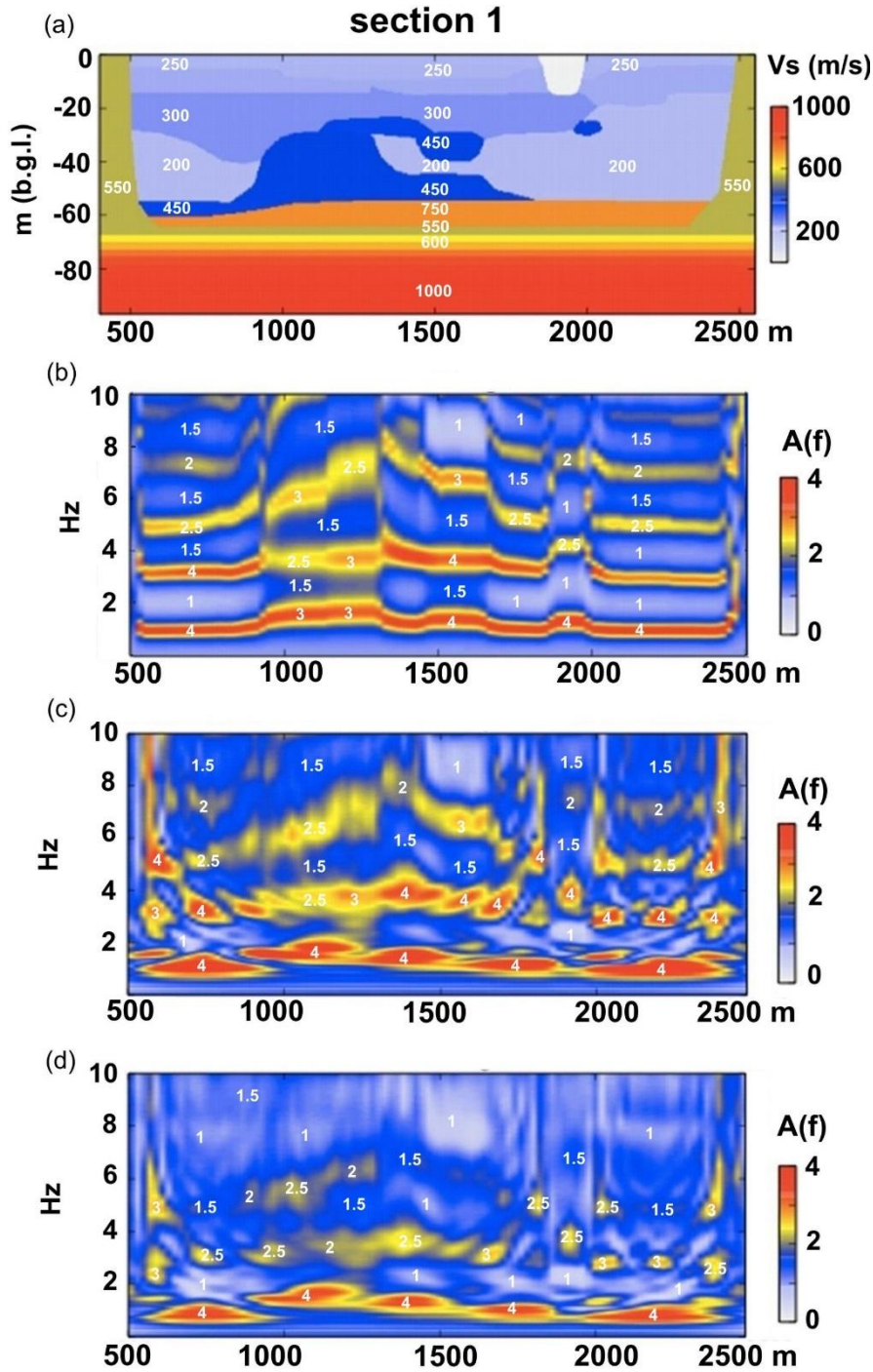
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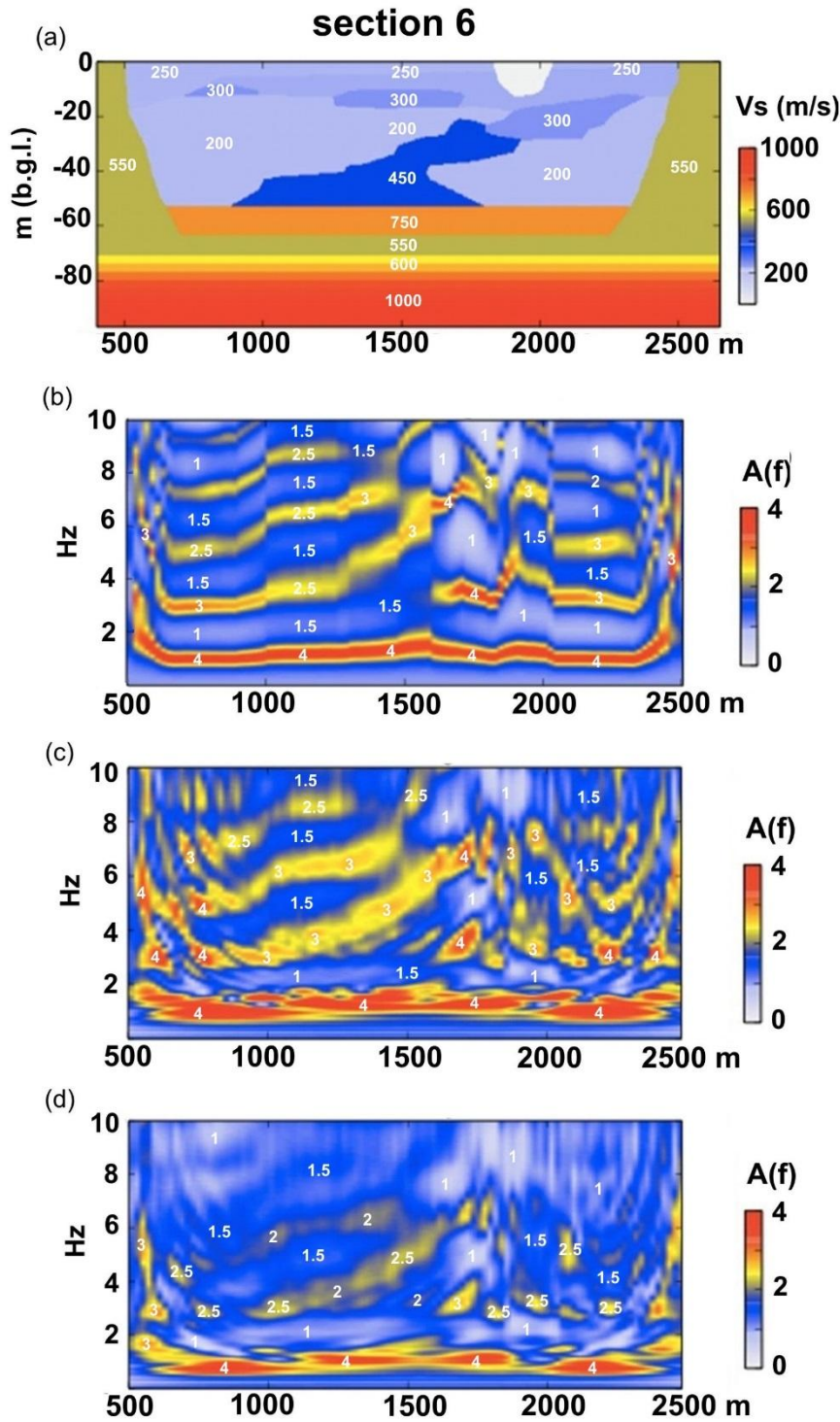
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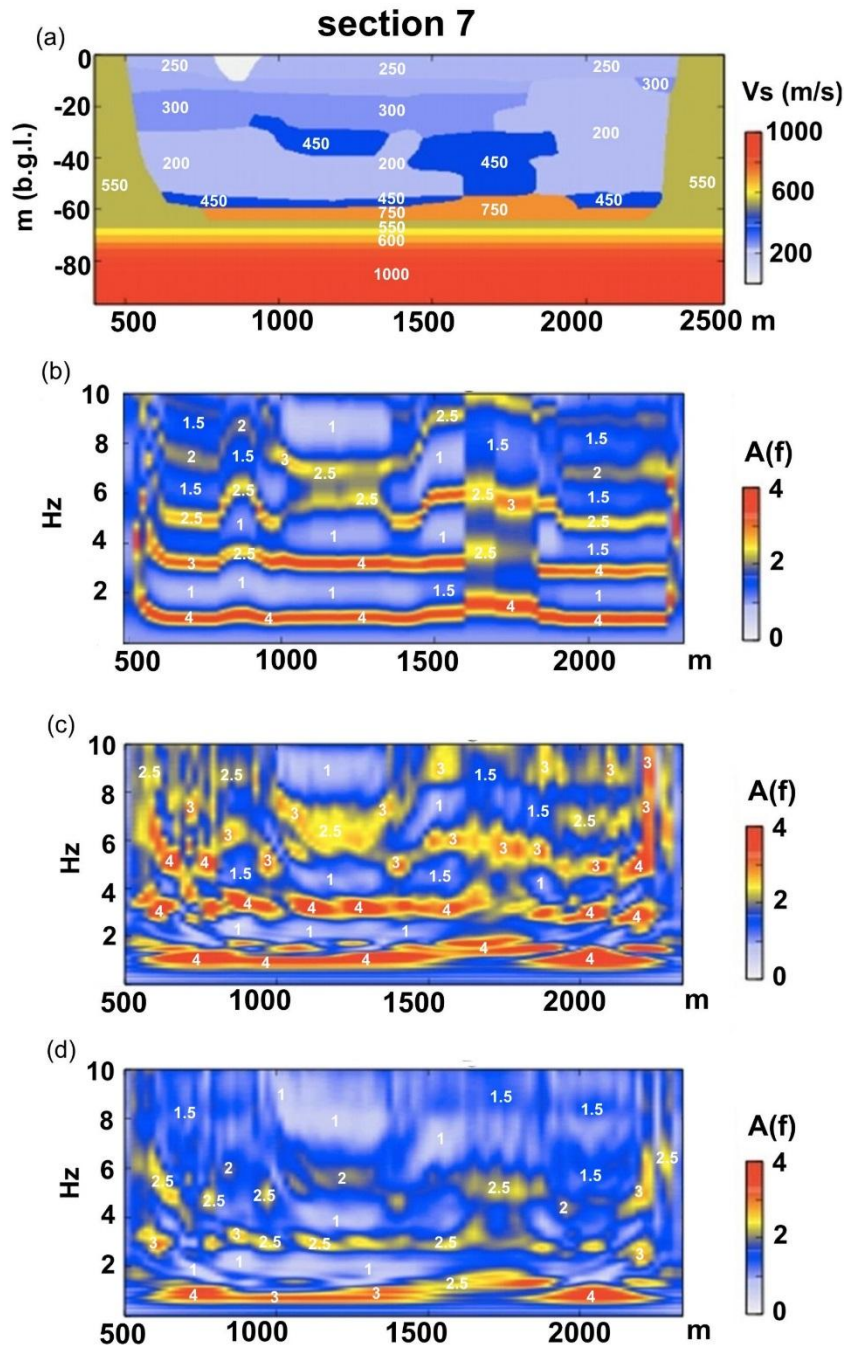
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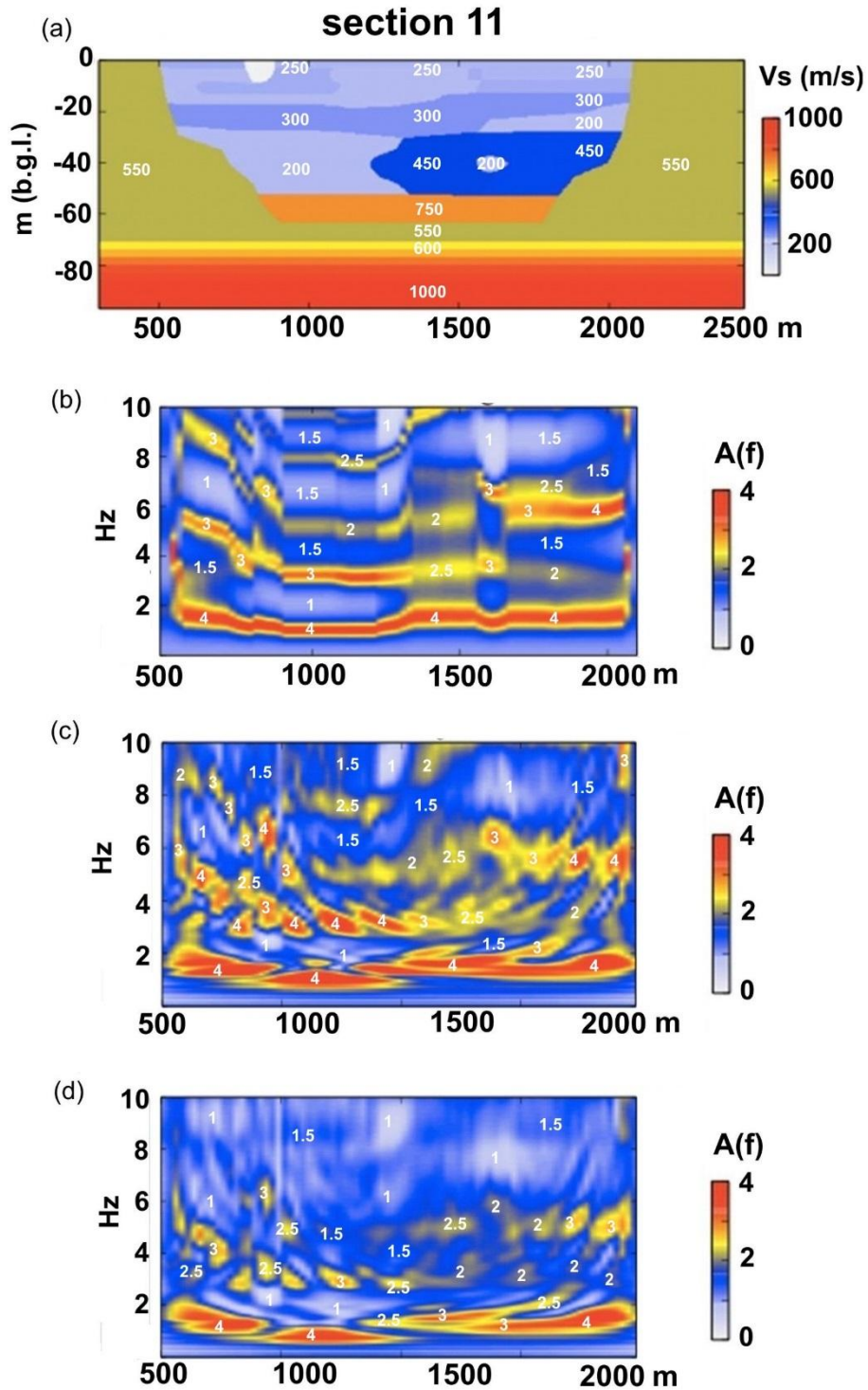
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957 Fig.11 – Outputs of the 2D numerical model performed along section 6 of Fig.7: a) Vs value
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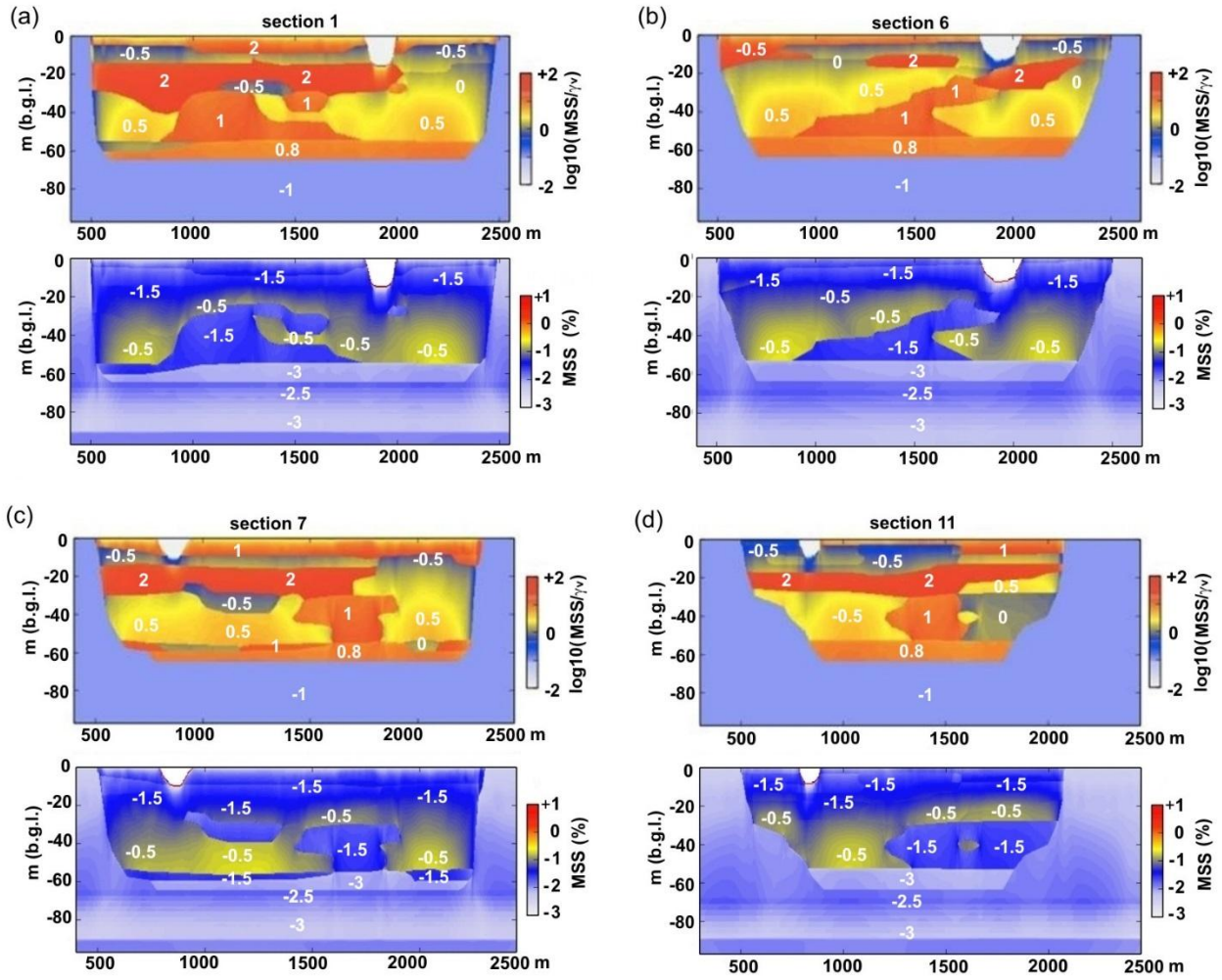
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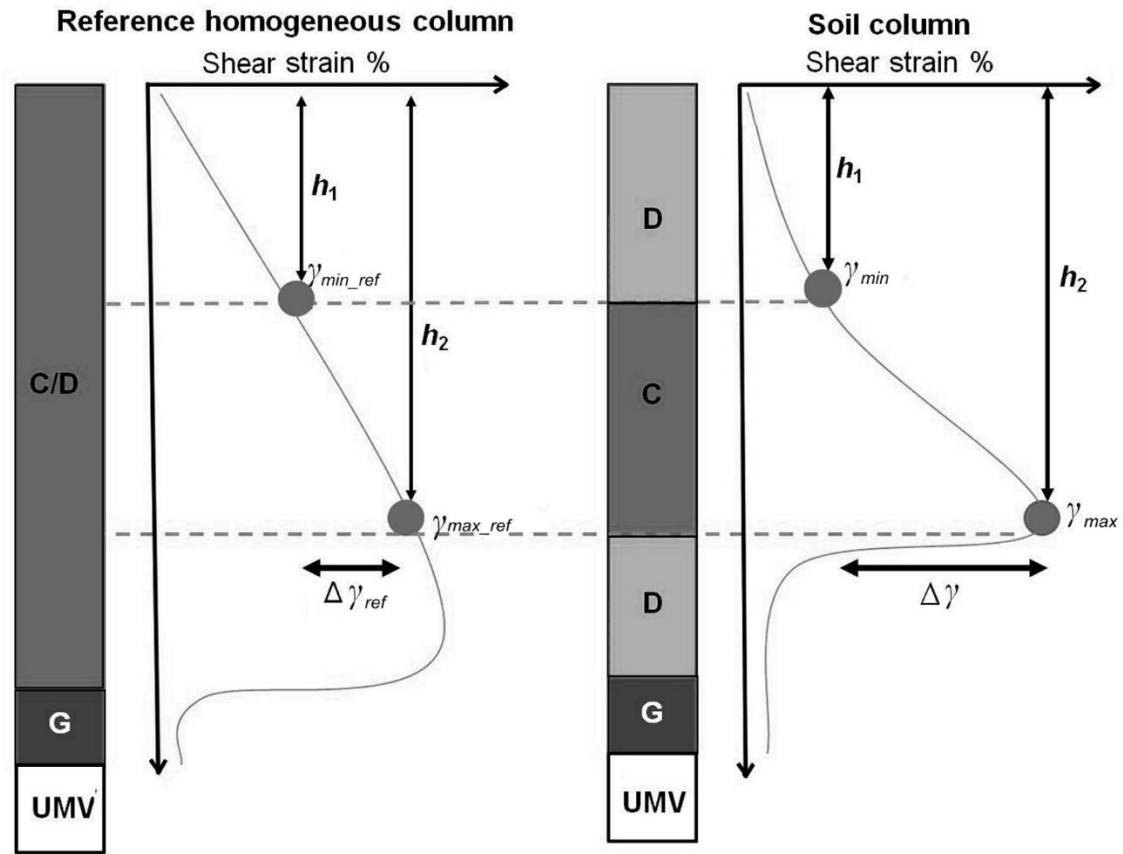
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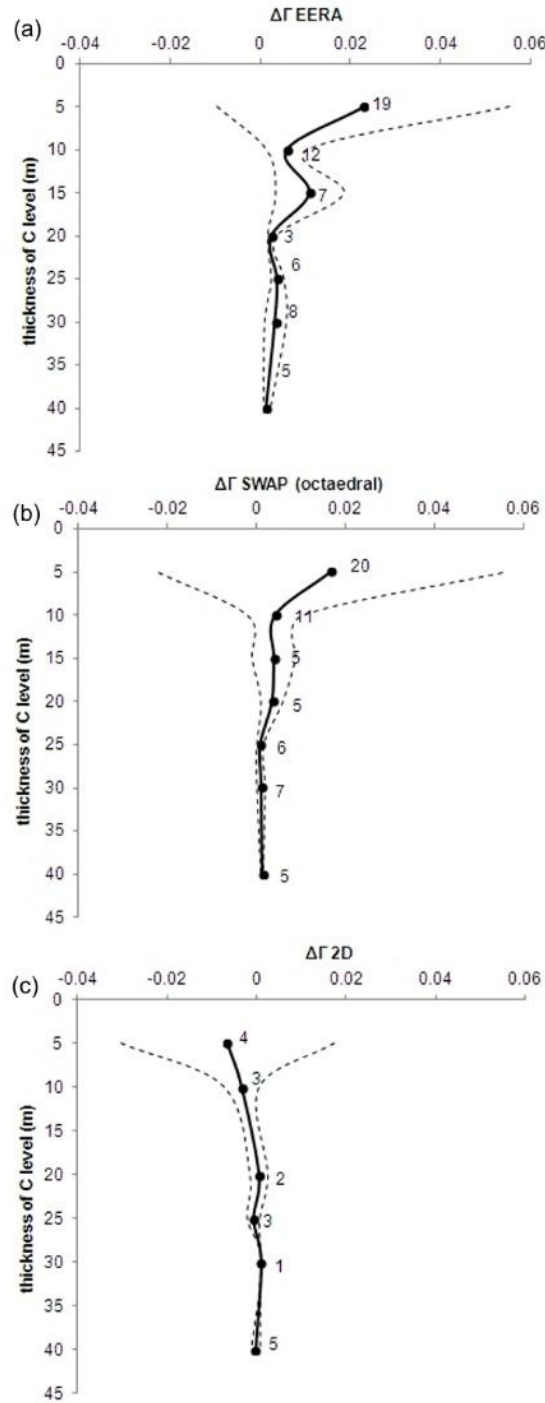
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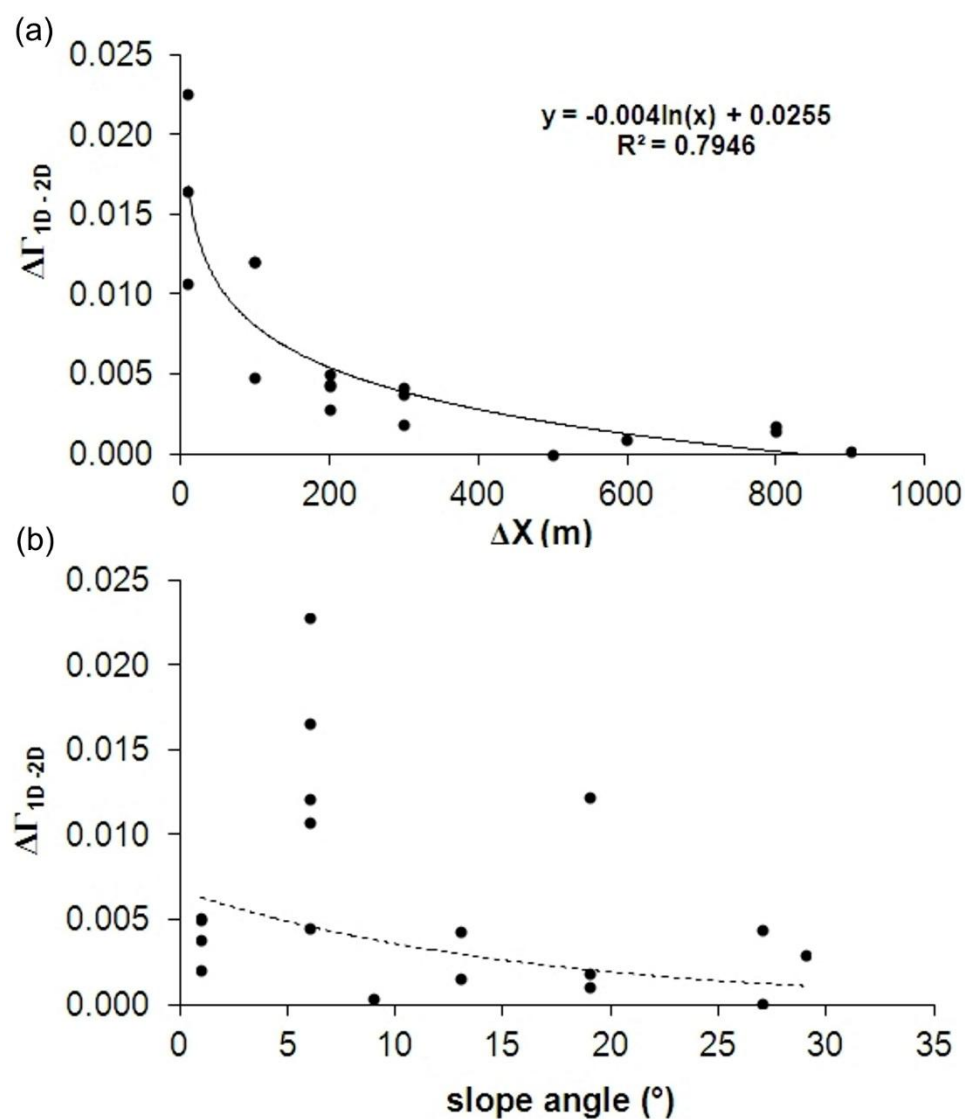
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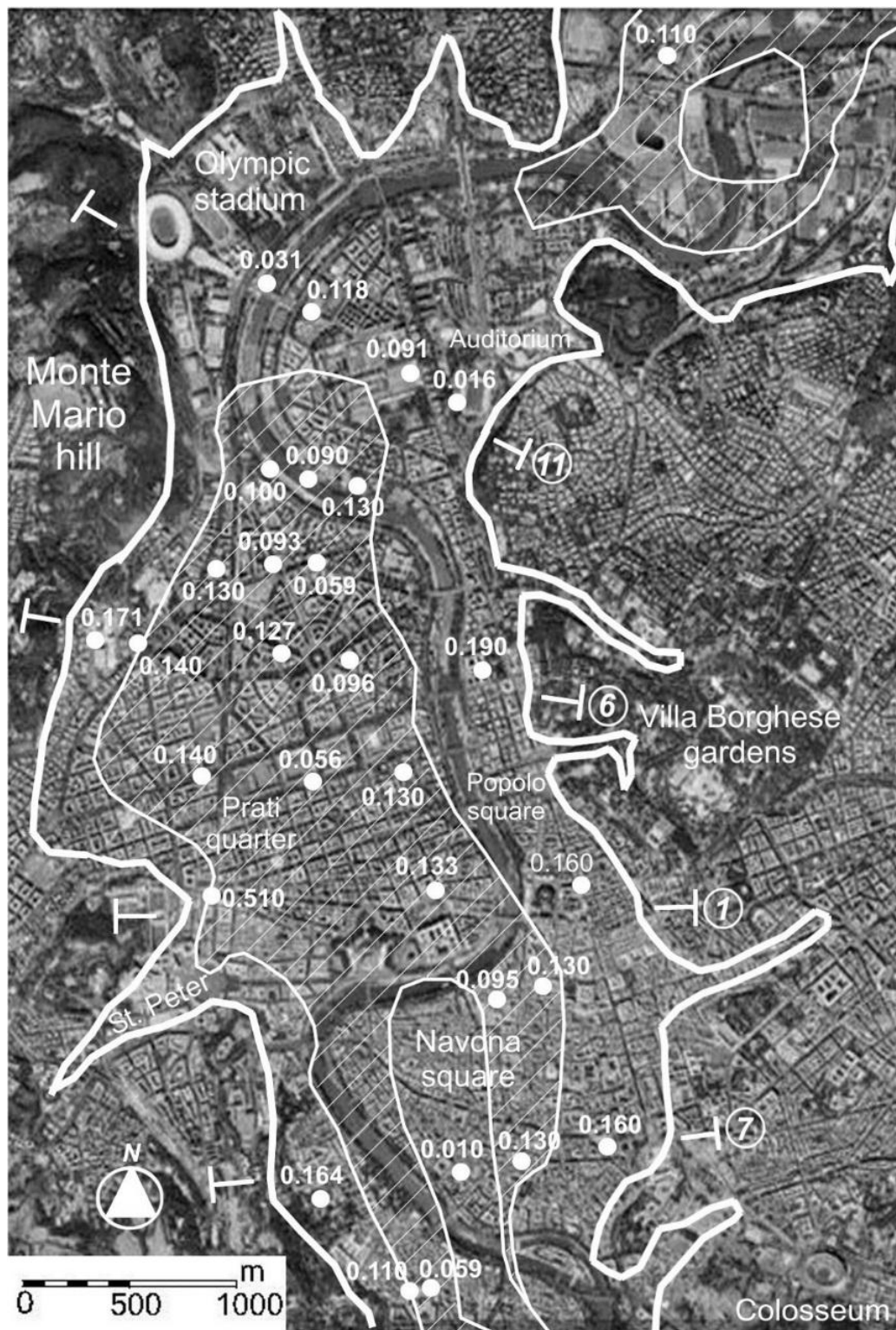
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 992 for the 475-years earthquake scenario are also reported.

n°	ID	number of layers	total thickness (m)	soil column stratigraphy (lithotechnical level, thickness (m))									% clay	% sand	soil composition of the reference
1	2B	8	70.0	R, 10	A2, 5	A1, 5	B1, 15	D1, 10	C, 5	D1, 10	G, 10		21	79	D
2	5B	8	65.0	R, 5	A2, 5	A1, 10	B1, 5	D1, 5	C, 10	D1, 15	G, 10		38	62	D
3	9A	8	65.0	R, 10	A1, 5	A2, 5	B1, 5	C, 5	D1, 10	C, 15	G, 10		46	54	D
4	12E	8	62.5	R, 2.5	A1, 10	A2, 5	C, 10	D1, 10	C, 5	D1, 10	G, 10		48	52	D
5	3C	8	62.5	R, 2.5	A2, 5	A1, C,	B1, 5	C, 5	D1, 20	C, 10	G, 10		40	60	D
6	5C	8	62.5	R, 2.5	A1, 5	A2, 5	B1, 10	C, 5	D1, 10	C, 15	G, 10		48	52	D
7	6D	8	62.5	R, 2.5	A2, 10	B2, 5	C, 5	D1, 15	C, 5	D1, 10	G, 10		32	68	D
8	10A	8	60.0	R, 5	A1, 5	C, 5	B2, 5	D1, 5	D2, 15	C, 10	G, 10		58	42	C
9	9D	8	60.0	R, 5	A1, 5	A2, 5	C, 5	D1, 5	C, 15	D1, 10	G, 10		50	50	C
10	11D	8	57.5	R, 2.5	A2, 5	B1, 10	C, 5	D2, 10	C, 5	D1, 10	G, 10		43	57	D
11	2D	7	67.5	R, 7.5	A2, 10	C, 5	B1, 5	C, 5	D1, 25	G, 10			30	70	D
12	9C	7	67.5	R, 7.5	A1, 10	B1, 15	D1, 10	C, 5	D1, 10	G, 10			33	67	D
13	10D	7	62.5	R, 2.5	A2, 5	A1, 10	B1, 10	D1, 10	C, 15	G, 10			48	52	D
14	10B	7	62.5	R, 2.5	A2, 5	A1, 5	C, 10	D2, 20	C, 10	G, 10			64	36	C
15	10C	7	62.5	R, 2.5	A2, 10	B2, 5	C, 5	D1, 30	D2, 5	G, 5			32	68	D
16	12C	7	62.5	R, 2.5	A2, 5	B2, 5	A2, 5	C, 20	D1, 15	G, 10			48	52	D
17	12D	7	62.5	R, 2.5	A2, 5	B2, 5	A2, 5	C, 10	D1, 25	G, 10			32	68	D
18	5A	7	62.5	R, 2.5	A2, 5	A1, 5	C, 10	B1, 5	C, 25	G, 10			88	12	C
19	9E	7	62.5	R, 7.5	A1, 5	C, 5	D1, 5	C, 20	D1, 10	G, 10			64	36	C
20	8D	6	65.0	R, 5	A1, 5	B2, 10	C, 10	D1, 25	G, 10				23	77	D
21	8E	6	65.0	R, 5	A1, 10	B1, 15	D1, 10	C, 15	G, 10				38	62	D
22	11B	6	62.5	R, 2.5	A1, 15	B1, 10	D1, 15	C, 10	G, 10				40	60	D
23	12B	6	62.5	R, 2.5	A2, 5	B2, 5	C, 30	D1, 10	G, 10				56	44	C
24	1A	6	62.5	R, 2.5	A2, 10	B2, 25	C, 15	D2, 5	G, 5				48	52	D
25	2C	6	62.5	R, 2.5	A1, 10	A2, 5	C, 5	D1, 30	G, 10				32	68	D
26	3A	6	62.5	R, 2.5	A1, 10	A2, 5	B1, 10	C, 30	G, 5				72	28	C
27	3B	6	62.5	R, 2.5	A2, 5	A1, 5	B1, 15	C, 30	G, 5				64	36	C
28	6C	6	62.5	R, 2.5	A2, 10	B2, 5	C, 20	D1, 15	G, 10				48	52	D
29	7A	6	62.5	R, 2.5	A1, 10	B1, 15	C, 25	D2, 5	G, 5				64	36	C
30	8A	6	62.5	R, 2.5	A2, 5	B2, 5	C, 30	D1, 10	G, 10				56	44	C
31	7B	6	60.0	R, 10	A2, 5	B2, 5	C, 10	D1, 25	G, 5				25	75	D
32	8C	6	60.0	A2, 5	A1, 5	B2, 5	C, 25	D1, 10	G, 10				58	42	C
33	10E	6	57.5	R, 2.5	A2, 5	A1, 5	B1, 15	C, 20	G, 10				52	48	C
34	11E	6	57.5	R, 2.5	A2, 5	B2, 10	C, 5	D2, 25	G, 10				60	40	C
35	2A	6	55.0	A2, 10	A1, 5	C, 5	D2, 5	C, 25	G, 5				90	10	C
36	6E	5	70.0	R, 10	A2, 10	B1, 10	C, 30	G, 10					57	43	C
37	3E	5	67.5	R, 2.5	A2, 10	C, 15	D1, 30	G, 10					37	63	D
38	11A	5	62.5	R, 2.5	A1, 15	B1, 10	C, 25	G, 10					64	36	C
39	1C	5	62.5	R, 2.5	A1, 10	B1, 15	C, 25	G, 10					56	44	C
40	6B	5	62.5	R, 2.5	A2, 5	B2, 5	C, 40	G, 10					72	28	C
41	9F	5	62.5	R, 7.5	A2, 5	C, 30	D1, 10	G, 10					56	44	C
42	8B	5	60.0	A1, 5	B2, 5	C, 30	D1, 10	G, 10					58	42	C
43	6A	4	62.5	R, 2.5	A2, 15	C, 40	G, 10						88	12	C
44	3D	4	60.0	A1, 15	C, 5	D1, 30	G, 10						33	67	D
45	1D	4	57.5	R, 2.5	A2, 10	C, 40	G, 5						86	14	C
46	7D	4	57.5	R, 7.5	C, 40	D1, 5	G, 5						69	31	C
47	12A	3	65.0	B2, 15	C, 40	G, 10							61	39	C
48	7C	3	60.0	R, 10	C, 40	G, 10							66	34	C

993

994 Tab.1 – Log-stratigraphies of the 48 soil columns located in Fig.1 which were derived from the 3D
995 engineering-geology model of the Tiber River alluvial deposits at Rome historical center and that
996 were used for the here performed 1D numerical modeling. The ID of each column is referred to
997 Fig.1b and the codes of the soil layers are referred to Fig.3. The corresponding reference columns
998 for the $\Delta\Gamma$ index computation are also indicated.